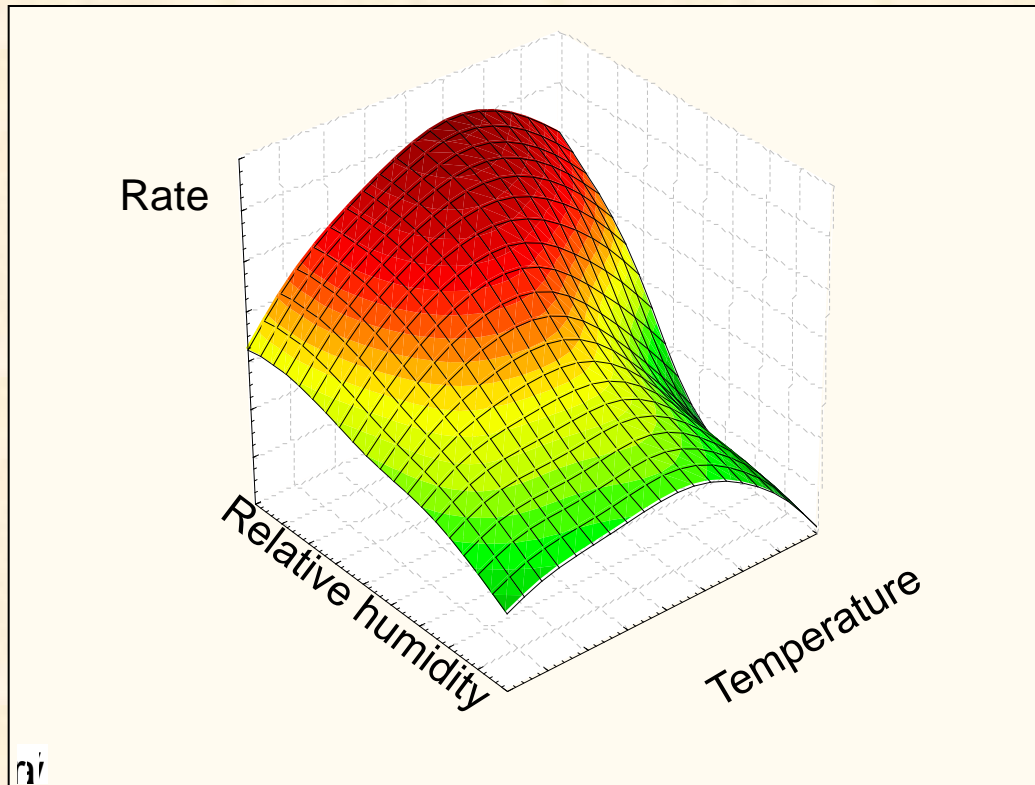


# Temperature

# Effect of conditions

- ▶ all conditions affect population growth via controlling metabolic processes in ectotherms
- ▶ temperature, humidity, day length, pH, etc.

*Lepidoglyphus* sp.



# Universal effect of temperature

- ▶ with respect to body temperature: cold-blooded / warm-blooded
- ▶ with respect to temperature change: poikilotherms / homoiotherms
- ▶ with respect to production of temperature: endotherms / ectotherms

▶ temperature affects population growth of ectotherms  $Q_{10} = 2.5$   
- rate of metabolism increases approx. by 2.5x for every 10 °C

▶ physiological time – combination of time and temperature

▶ rate of metabolism  $B$ :  $B \sim e^{-\beta/T}$   
( $T$  .. temperature)

- rate increases with body mass ( $M$ ):  
*per mass unit ...*

$$\frac{B}{M} \sim M^{1/4}$$

- biological time  $t_b$ :  $t_b \sim M^{1/4} e^{\beta/T}$

# Linear model

- ▶ model is based on the assumption that developmental rate is a linear function of temperature  $T$
- ▶ valid for the region of moderate temperatures (15-25°)
- ▶ at low temperatures organisms die due to coldness

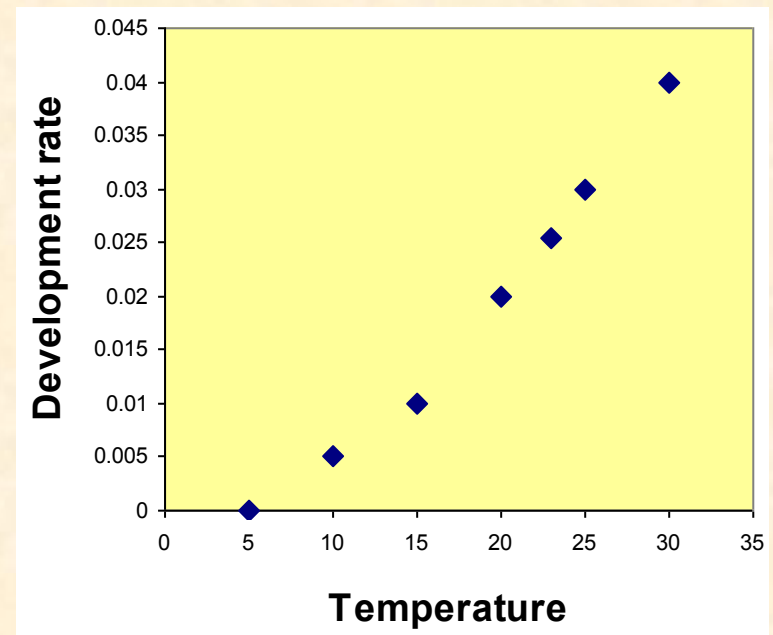
$D$  .. development time (days)

$v$  .. rate of development =  $1/D$

$T_{\min}$  .. lower temperature limit

- temperature at which

developmental rate = 0



$ET$ .. effective temperature .. developmental temperature between  $T$  and  $T_{\min}$   
 $S$  .. sum of effective temperature .. number of day-degrees [ $^{\circ}\text{D}$ ] required to complete development

.. does not depend on temperature =  $D*ET$

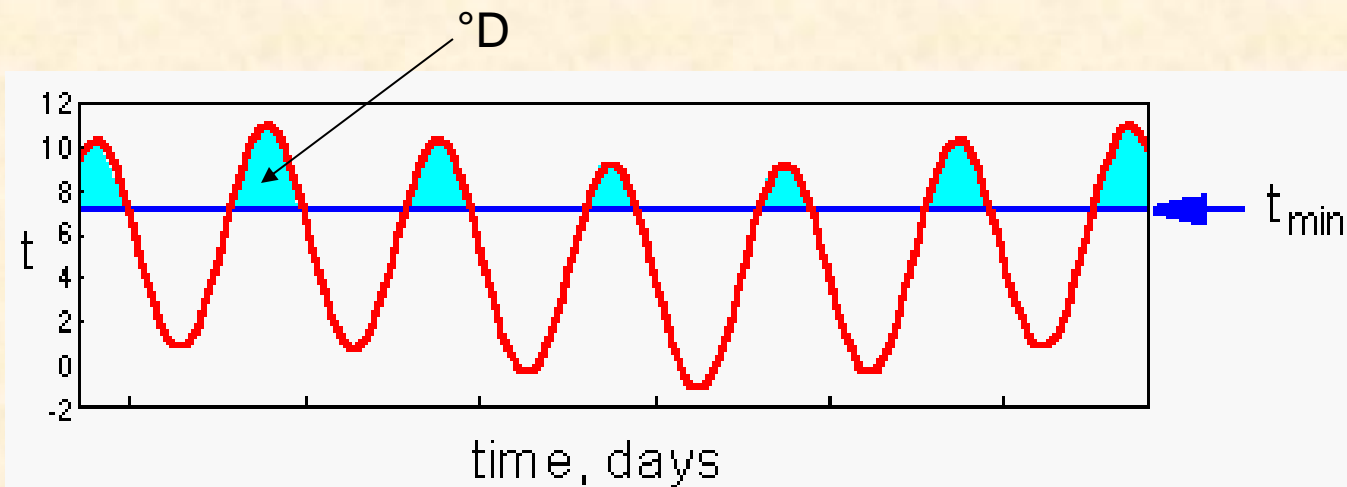
$T_{\min}$  and  $S$  can be estimated from the regression line of  $v = a + bT$

$$T_{\min} : \quad a + bT = 0 \quad \rightarrow \quad T_{\min} = -\frac{a}{b}$$

$$S : \quad S = D(T - T_{\min}) = D\left(T + \frac{a}{b}\right)$$

$$D = \frac{1}{v} = \frac{1}{a + bT} \quad \rightarrow \quad S = \frac{T + a/b}{a + bT} \quad \rightarrow \quad S = \frac{1}{b}$$

- ▶ sum of effective temperature ( $S$ ) [ $^{\circ}\text{D}$ ] is equal to area under temperature curve restricted to the interval between current temperature ( $T$ ) and  $T_{\min}$
- ▶ biofix .. the date when day-degrees begin to be accumulated

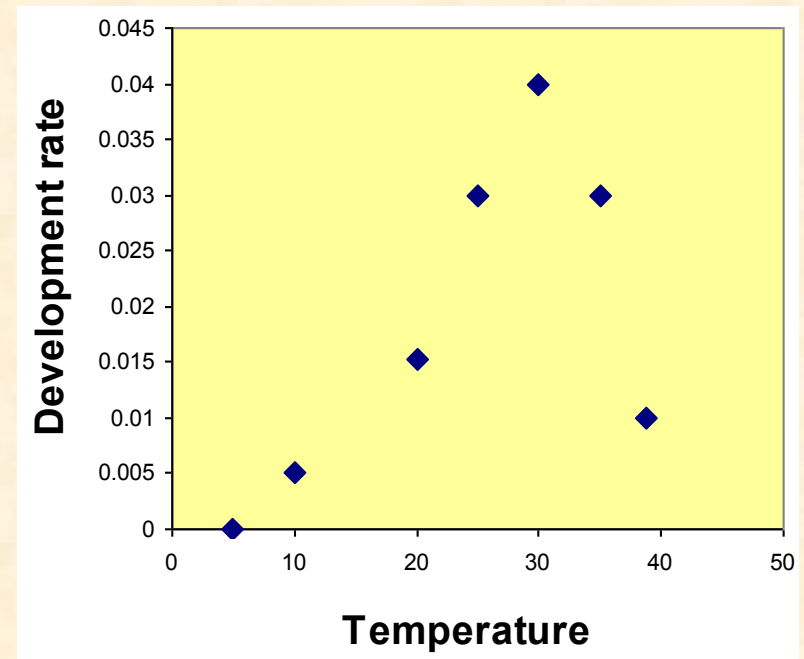


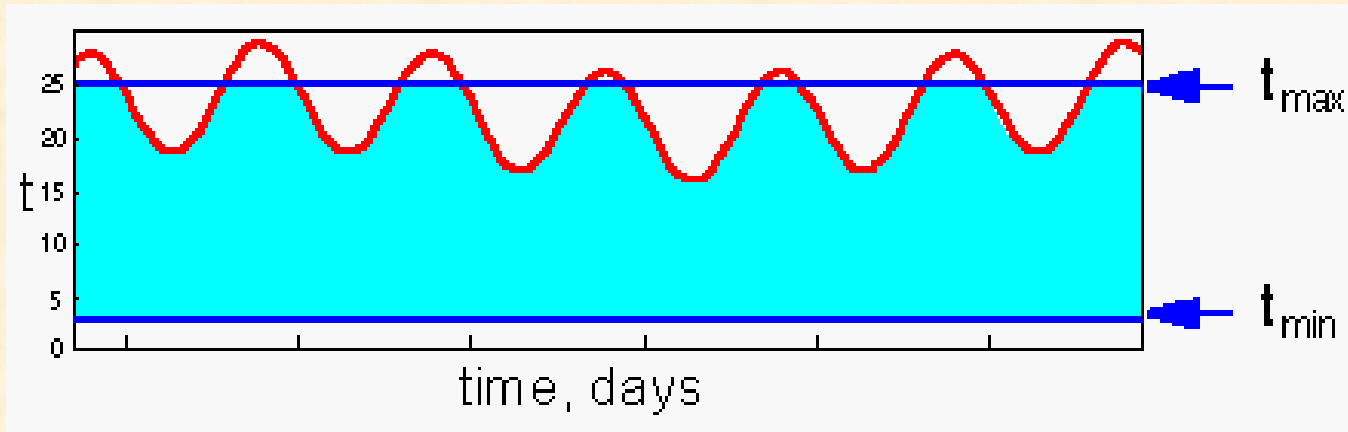
$$S = \sum_{i=1}^n T - T_{\min}$$

# Non-linear models

- ▶ when development rate is a non-linear function of temperature
- ▶  $ET$ .. developmental temperature between  $T_{\min}$  and  $T_{\max}$
- ▶ at high temperatures organisms die due to overheating

$T_{\max}$  .. upper temperature threshold  
- temperature at which  
developmental rate = 0





- ▶ several different non-linear models (Briere, Lactin, etc.)
- ▶ allow to estimate  $T_{\min}$ ,  $T_{\max}$  and  $T_{\text{opt}}$  (optimum temperature)
- ▶ easy to interpret for experiments with constant temperature
- ▶ instead of using average day temperature, use actual temperature



Briere et al. (1999)

$$v = a \times T \times (T - T_{\min}) \times \sqrt{T_{\max} - T}$$

$v$  .. rate of development ( $=1/D$ )

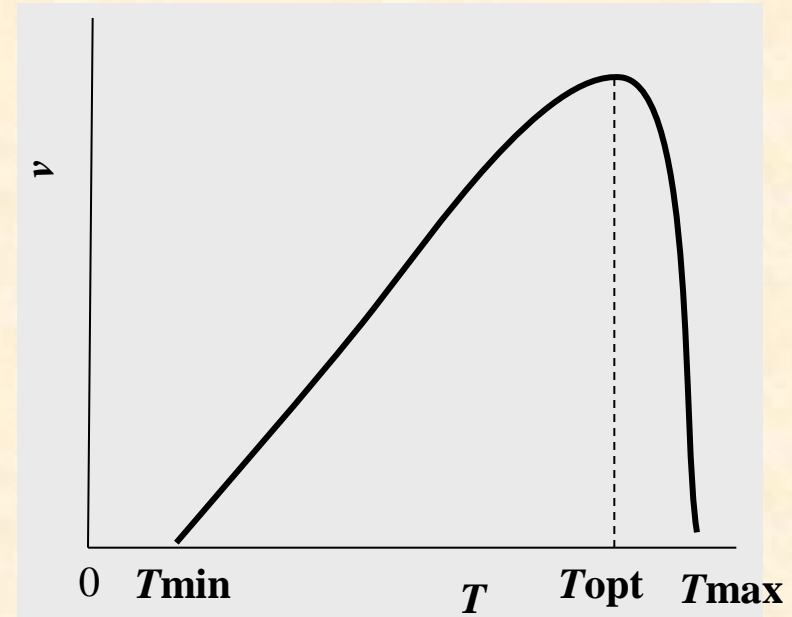
$T$  .. experimental temperature

$T_{\min}$  .. low temperature threshold

$T_{\max}$  .. upper temperature threshold

$a$  .. unknown parameter

Optimum temperature:



$$t_{opt} = \frac{4T_{\max} + 3T_{\min} + \sqrt{16T_{\max}^2 + 9T_{\min}^2 - 16T_{\min}T_{\max}}}{10}$$

- ▶ parameters are estimated using non-linear regression

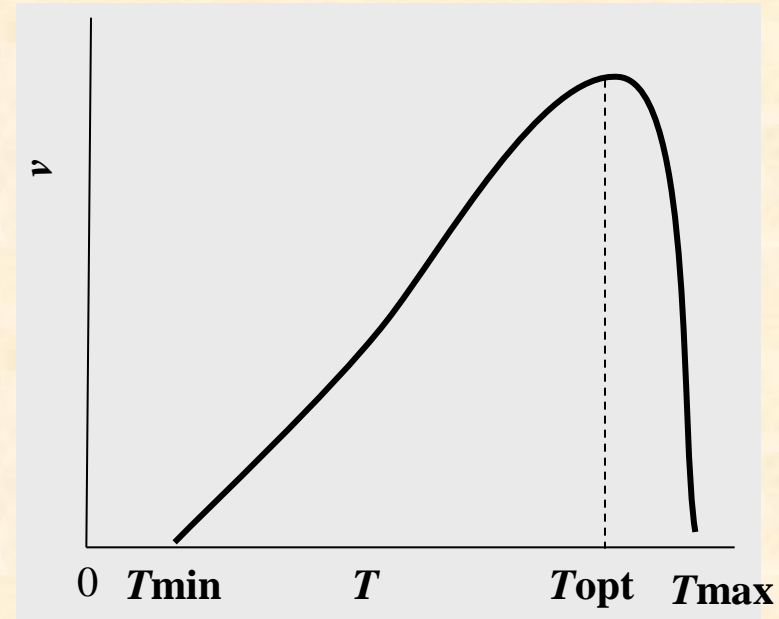
Lactin et al. (1995)

$$v = e^{\rho T} - e^{\left(\rho T_m - \frac{T_m - T}{\Delta}\right)} + \phi$$

$v$  .. rate of development

$T$  .. experimental temperature

$T_m$ ,  $\Delta$ ,  $\rho$ ,  $\phi$  .. unknown parameters



$T_{\max}$  and  $T_{\min}$  can be estimated from the formula:

$$0 = e^{\rho T} - e^{\left(\rho T_m - \frac{T_m - T}{\Delta}\right)} + \phi$$

$T_{\text{opt}}$  can be estimated from the first derivative:

$$\frac{\partial v(T)}{\partial T} = \rho e^{\rho T} - \frac{1}{\Delta} e^{\rho T_m - \frac{T_m - T}{\Delta}}$$