

$$1) g: \mathbb{R} \rightarrow \mathbb{R}; g(x) = |3-x| - |x+2| - 1$$

$$\begin{aligned} a) 3-x=0 & \quad x+2=0 \quad \rightarrow \text{intervaly: } (-\infty, -2), (-2, 3), (3, \infty) \\ x=3 & \quad x=-2 \end{aligned}$$

$(-\infty, -2)$

$$g(x) = 3-x - [-(x+2)] - 1$$

$$g(x) = 3-x+x+2-1$$

$$\underline{g(x) = 4} \quad \checkmark$$

$(-2, 3)$

$$g(x) = 3-x - (x+2) - 1$$

$$g(x) = 3-x-x-2-1$$

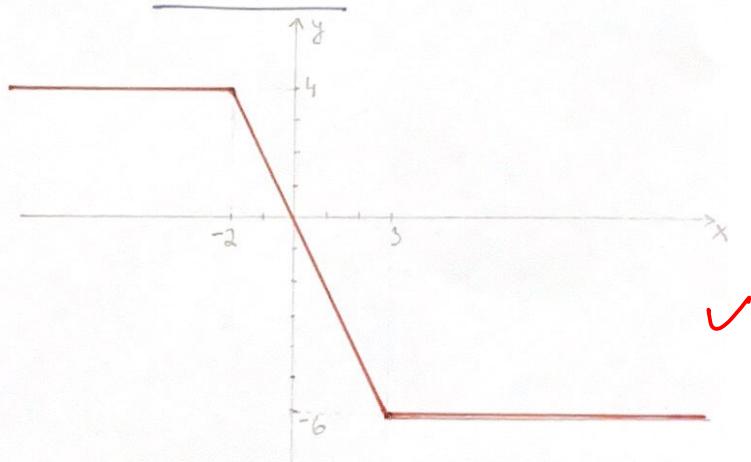
$$\underline{g(x) = -2x} \quad \checkmark$$

$(3, \infty)$

$$g(x) = -(3-x) - (x+2) - 1$$

$$g(x) = -3+x-x-2-1$$

$$\underline{g(x) = -6} \quad \checkmark$$



$$b) H(f) \in (-6, 4) \rightarrow \text{Ize vidět z grafu} \rightarrow$$

$\checkmark b$

c) funkce g není rostoucí na žádném intervalu, je klesající na $(-2, 3)$
a konstantní na intervalech $(-\infty, -2)$ a $(3, \infty)$

$$d) |3-x| - |x+2| - 1 < 1 \rightarrow \text{intervaly } (-\infty, -2), (-2, 3), (3, \infty)$$

$$x \in (-\infty, -2)$$

$$x \in (-2, 3)$$

$$x \in (3, \infty)$$

$$3-x+x+2-1 < 1$$

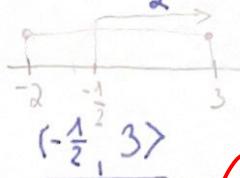
$$4 \cancel{<} 1$$

$$\underline{k = \emptyset}$$

$$3-x-x-2-1 < 1$$

$$-2x < 1$$

$$x > -\frac{1}{2}$$



$$-3+x-x-2-1 < 1$$

$$-6 < 1$$

$$x \in \mathbb{R}$$

$$\underline{(3, \infty)}$$

$$\underline{x \in (-\frac{1}{2}, \infty)} \quad \checkmark$$

\checkmark Celkem 5 b