



Introduction to EM



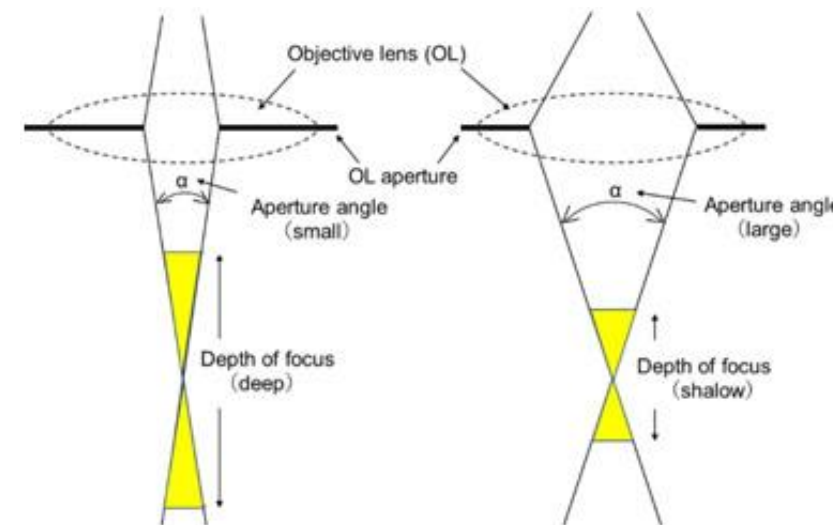
INSTITUTE OF PHYSICS OF MATERIALS
— Czech Academy of Sciences —

Light microscopy - limitation

resolution
magnification
depth of focus

$$d_d = 0.61 \lambda / \alpha$$

Abbe, Airy



visible light - $\lambda = 390 - 760$ nm

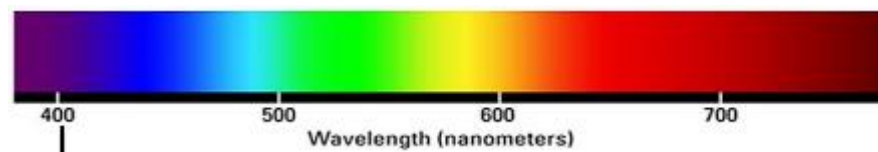




Table Electron Properties as a Function of Accelerating Voltage

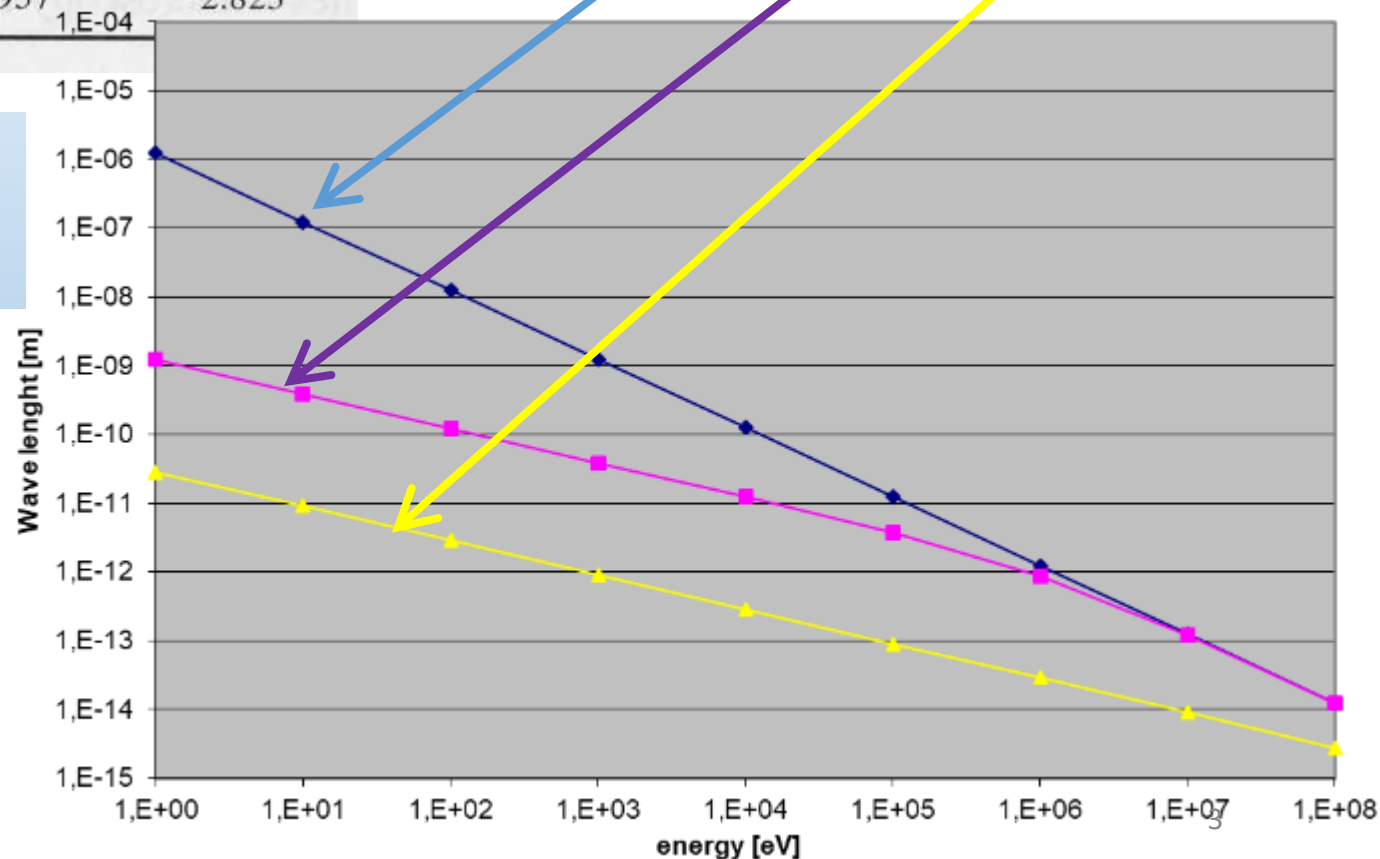
Accelerating voltage (kV)	Nonrelativistic wavelength (nm)	Relativistic wavelength (nm)	Mass ($\times m_0$)	Velocity ($\times 10^8$ m/s)
100	0.00386	0.00370	1.196	1.644
120	0.00352	0.00335	1.235	1.759
200	0.00273	0.00251	1.391	2.086
300	0.00223	0.00197	1.587	2.330
400	0.00193	0.00164	1.783	2.484
1000	0.00122	0.00087	2.957	2.823

$$\lambda = \frac{h}{\sqrt{2m_0eU\left(1 + \frac{eU}{m_0c^2}\right)}} \approx \frac{h}{\sqrt{2m_0eU}} \Rightarrow \lambda = \frac{1,226}{\sqrt{U}} [nm]$$

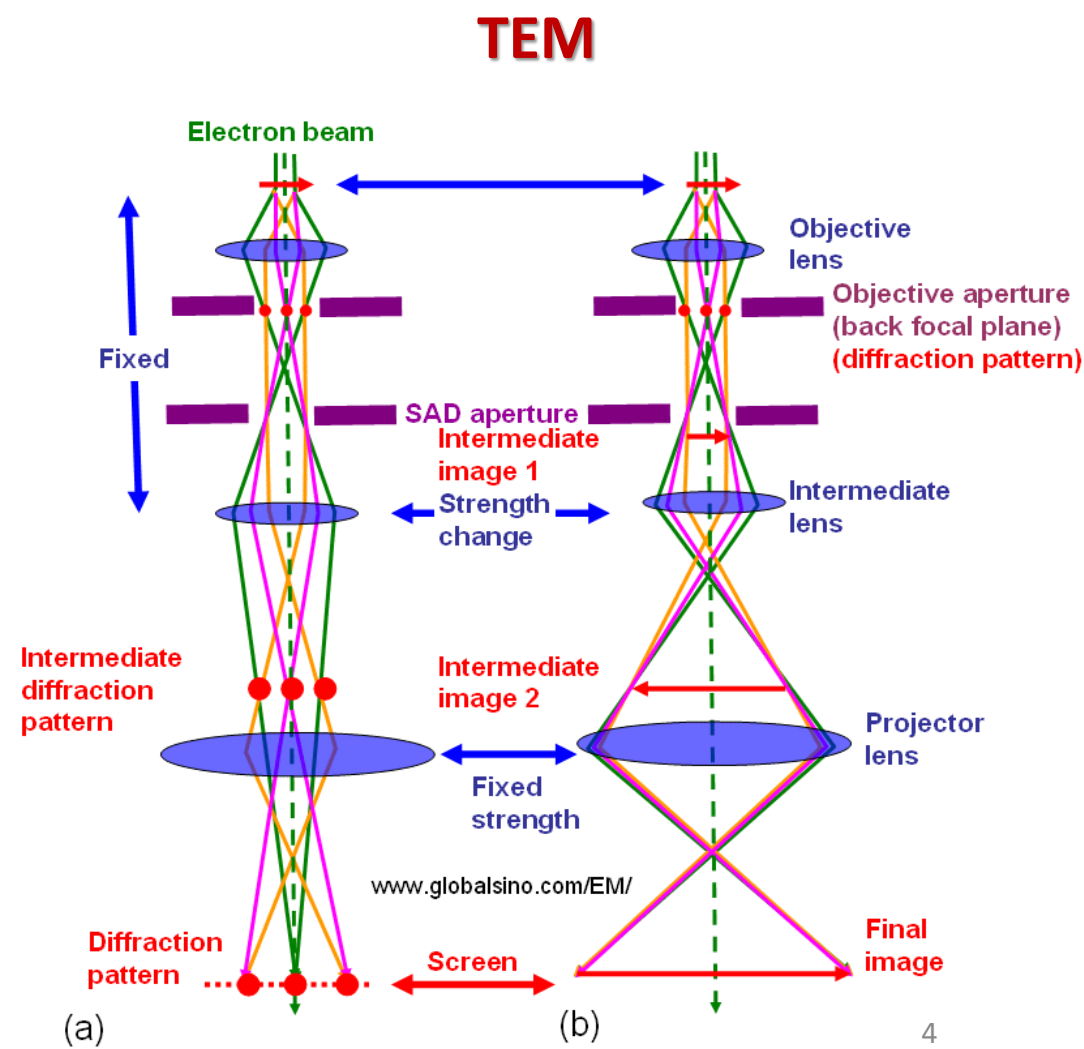
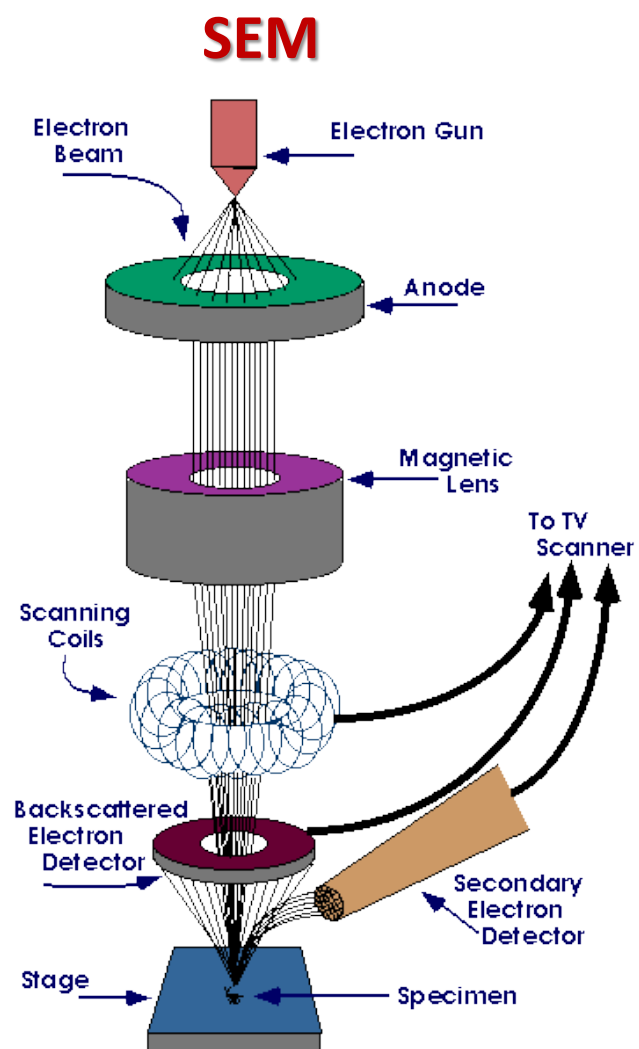
U=10kV (SEM) -> $\lambda = 0.01226$ nm

U=100kV (TEM) -> $\lambda = 0.0039$ nm

Visible light -> $\lambda = 390 - 760$ nm



Electron microscopy



Specimens

SEM

Conductive specimens! (C, Au coatings)

Polished or electropolished metallographic cuts

Fracture surfaces

Tensile, fatigue, creep,... specimens

Powders

TEM

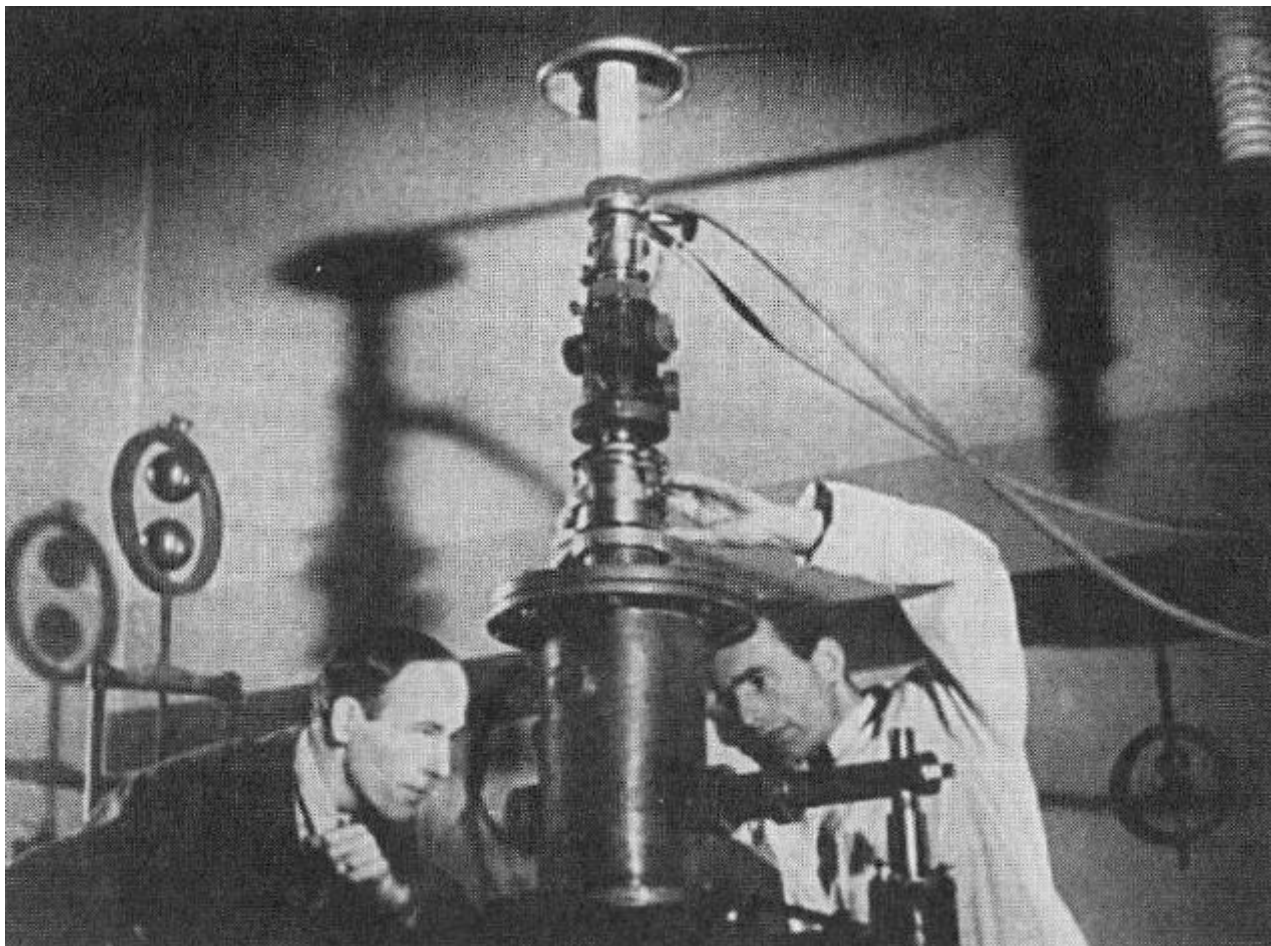
Specimens transparent for electrons! (~ 100 nm)

Thin foils – electropolished, Ar ions bombardment

Surface or extraction replica

Nanopowders

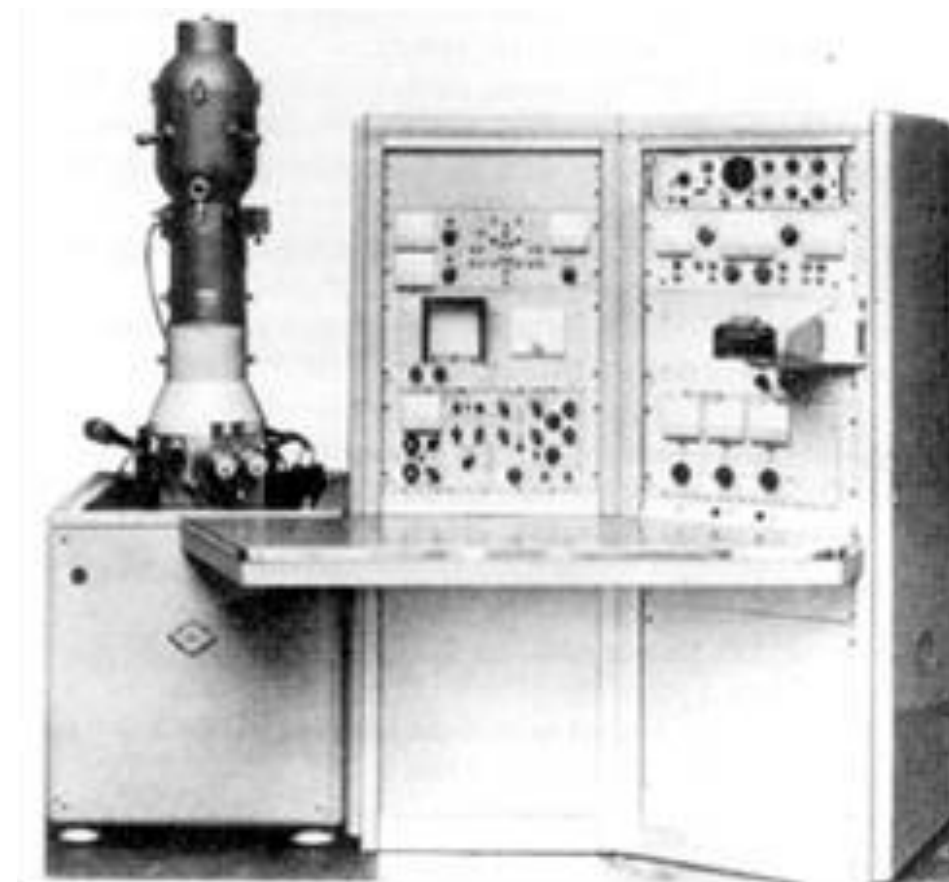
FIB



Berlin early 1930s: Ruska and Knoll

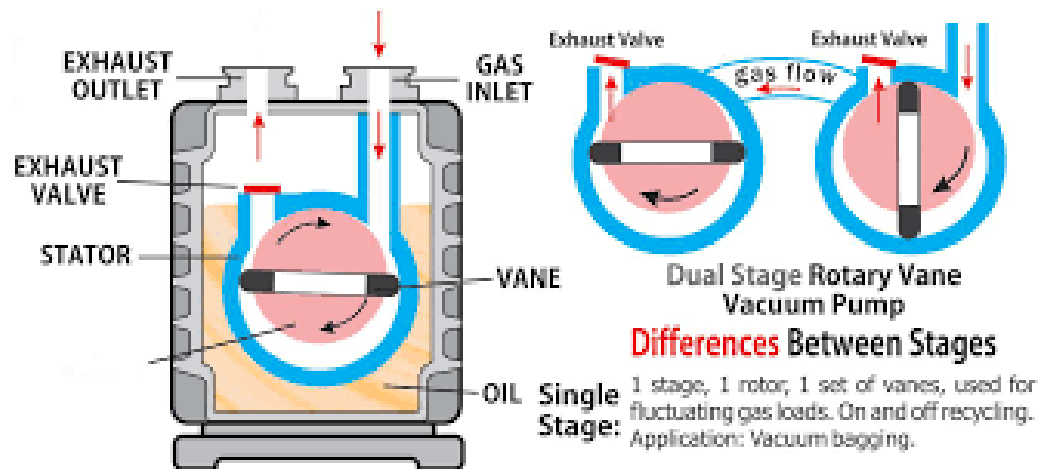
1931: 16x

1933: 12000x



1965: Oatley, first commercial SEM Stereoscan

Vacuum system



Rotary/scroll pump 10^{-1} Pa



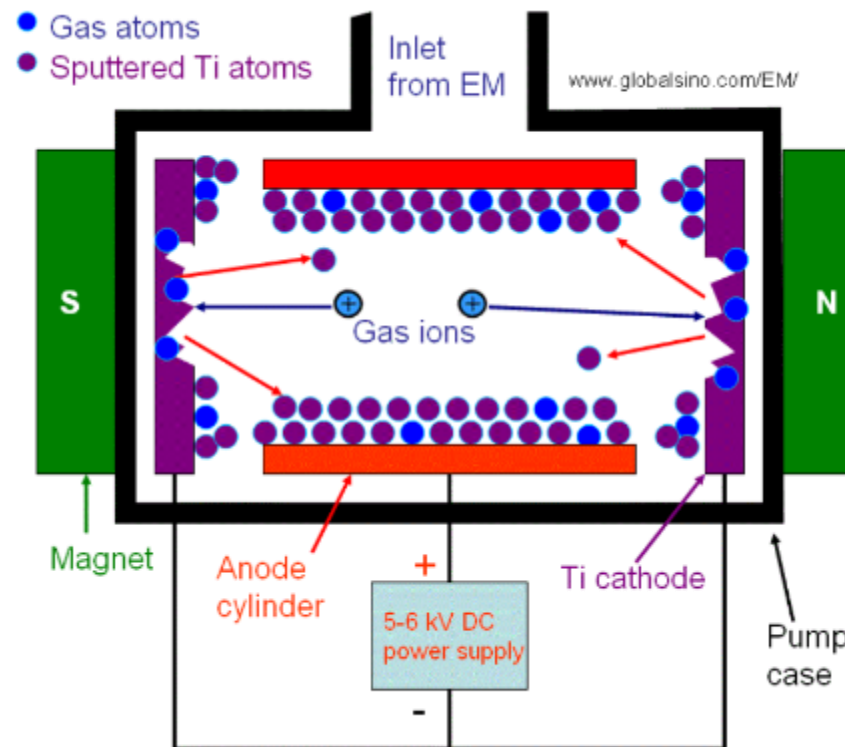
$10^{-2} - 10^{-9}$ Pa

Turbomolecular



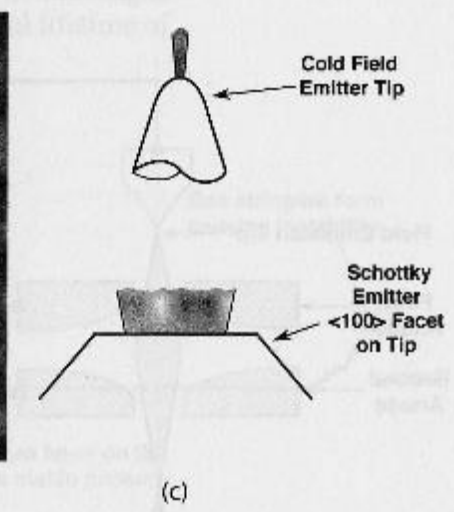
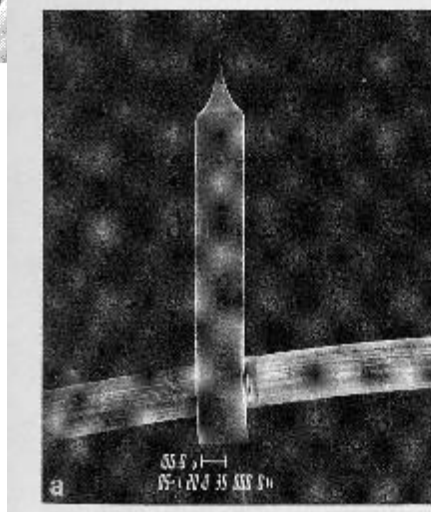
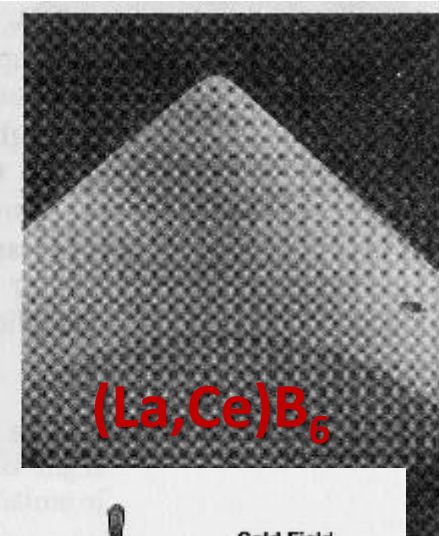
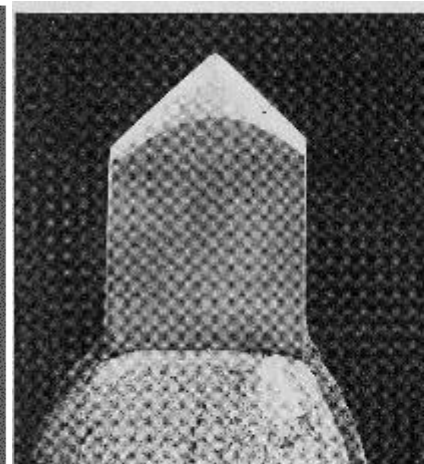
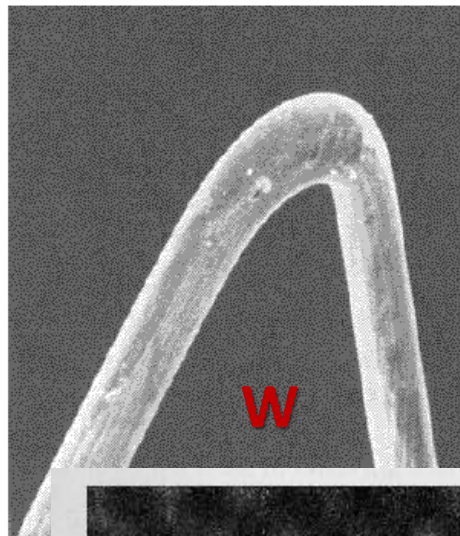
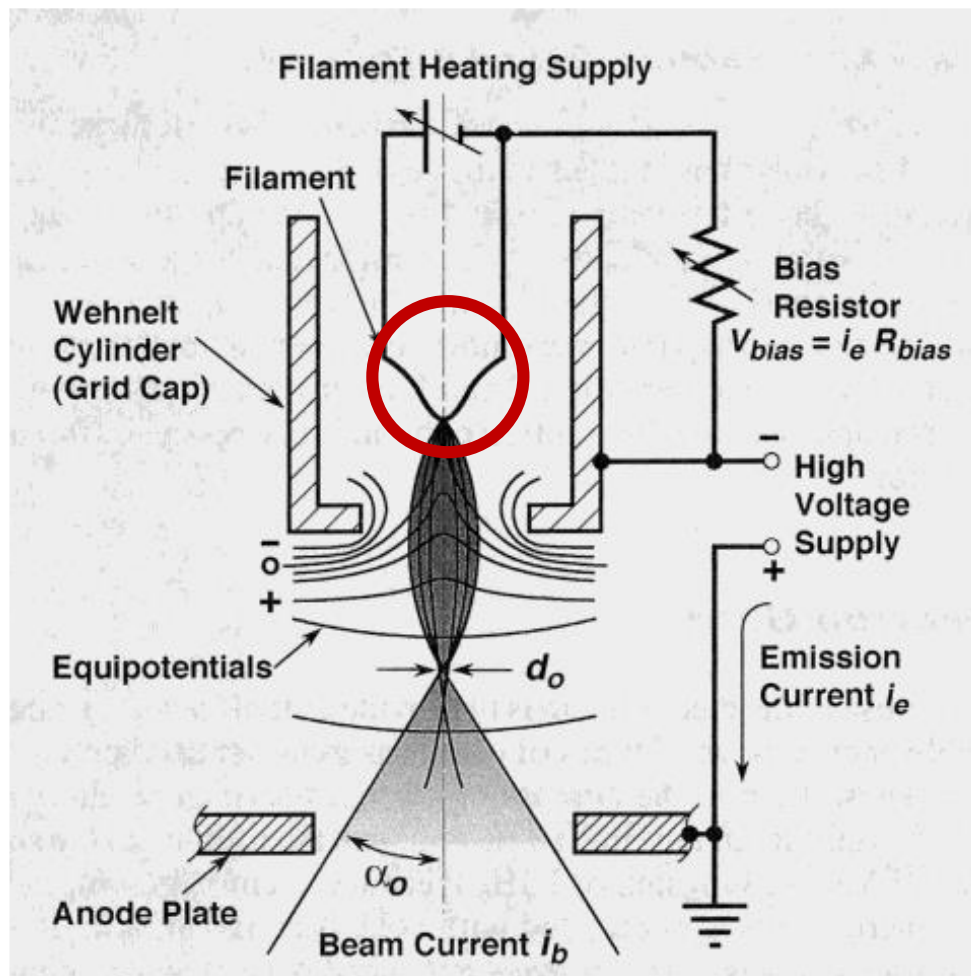
10^{-5} Pa

Diffusion pumps

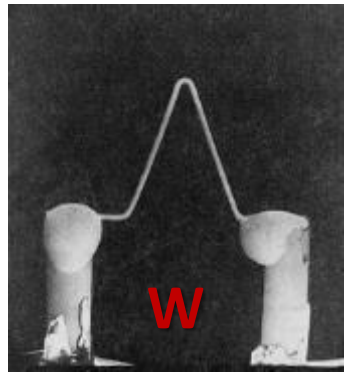


Ion pump 10^{-9} Pa

Electron sources



Field emission gun (FEG)
W wire + ZrO layer

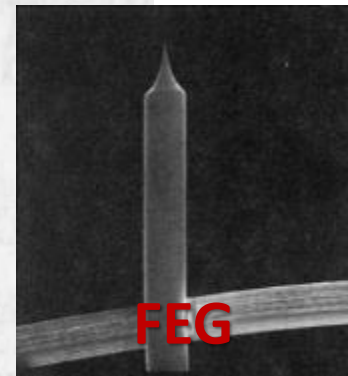


Electron sources



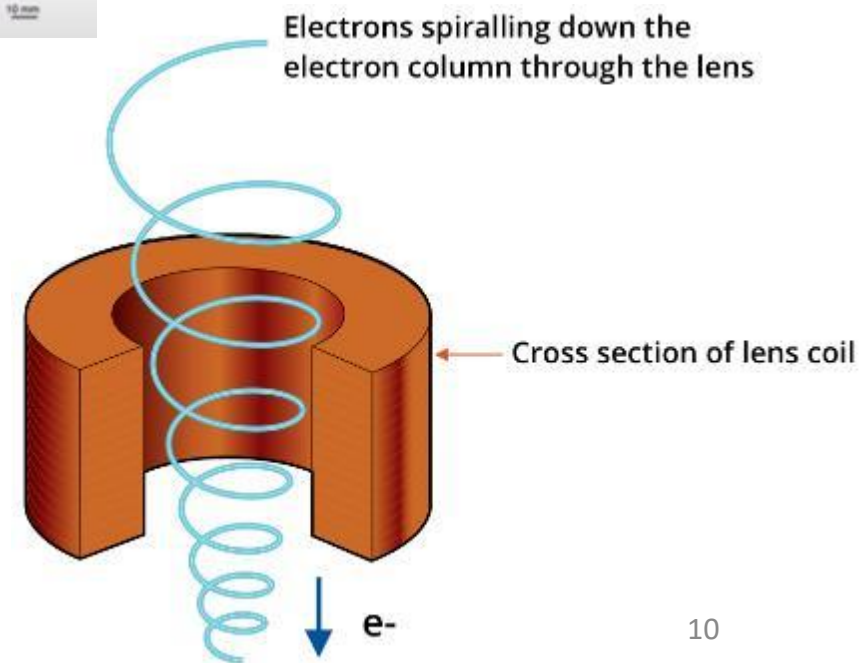
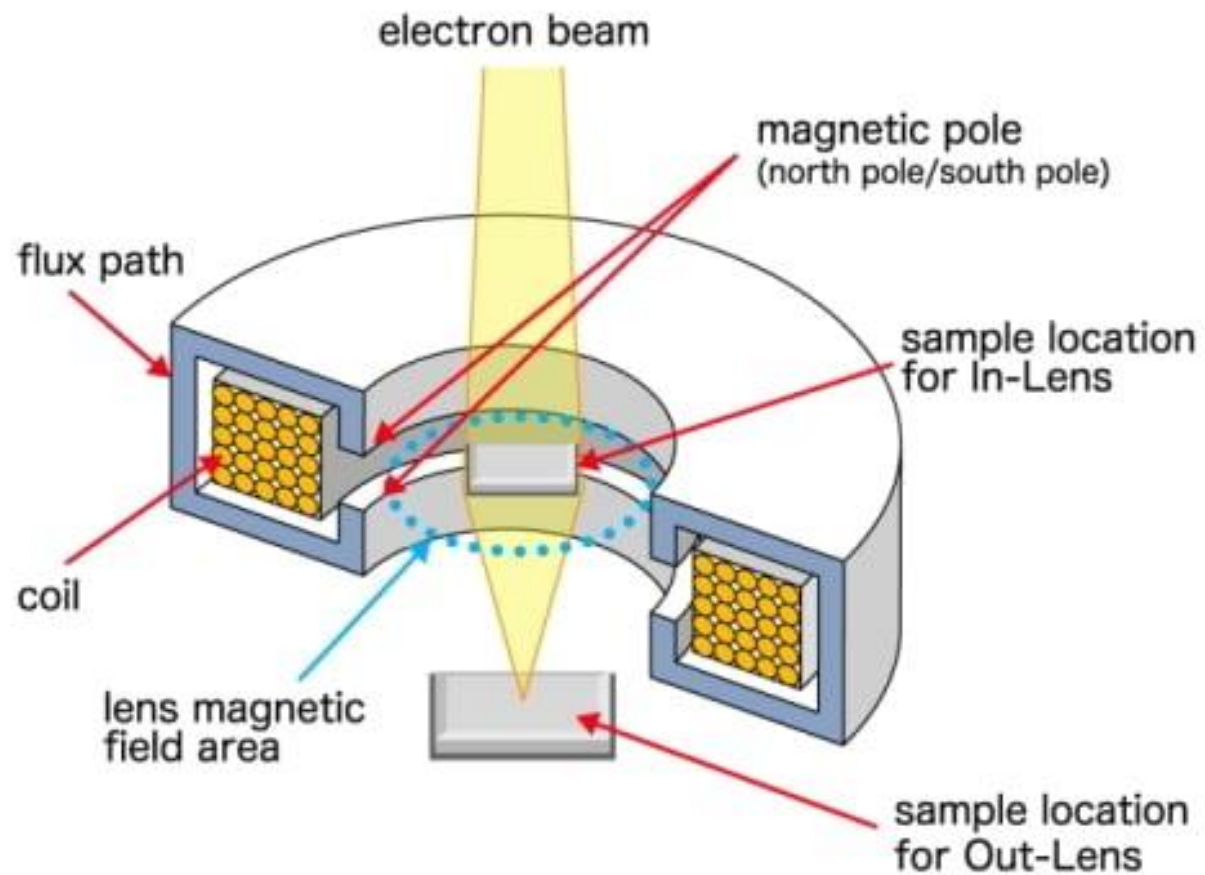
TABLE 5.1. Characteristics of the Three Principal Sources Operating at 100 kV

	Units	Tungsten	LaB ₆	Field Emission
Work function, Φ	eV	4.5	2.4	4.5
Richardson's constant	A/m ² K ²	6×10^5	4×10^5	
Operating temperature	K	2700	1700	300
Current density	A/m ²	5×10^4	10^6	10^{10}
Crossover size	μm	50	10	<0.01
Brightness	A/m ² sr	10^9	5×10^{10}	10^{13}
Energy spread	eV	3	1.5	0.3
Emission current stability	%/hr	<1	<1	5
Vacuum	Pa	10^{-2}	10^{-4}	10^{-8}
Lifetime	hr	100	500	>1000

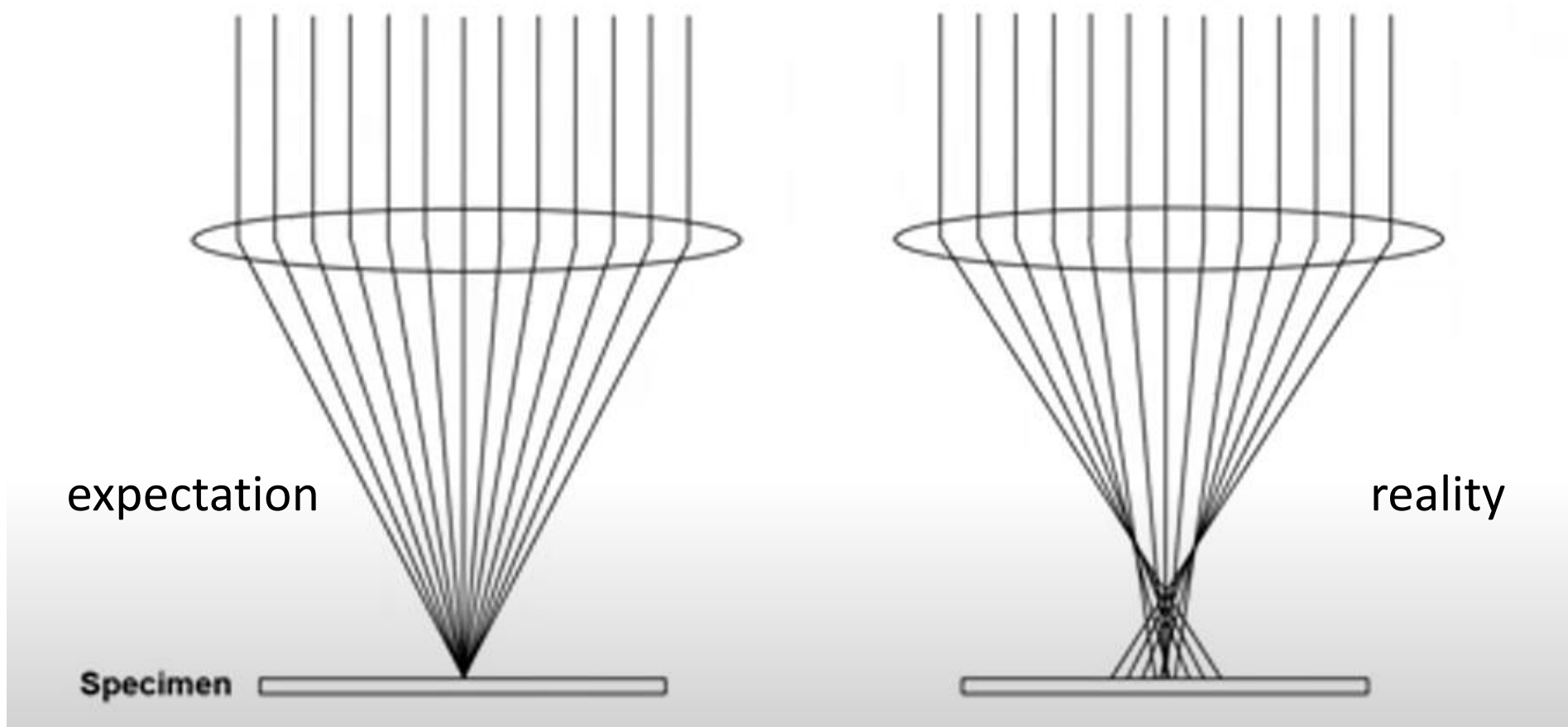


FEG
W wire +
ZrO layer

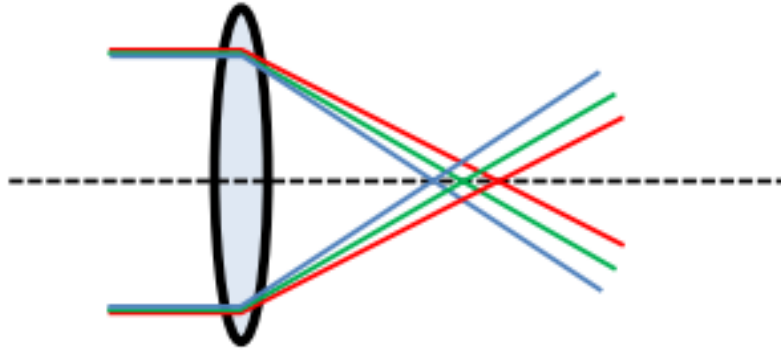
Magnetic lenses



Magnetic lenses – expectation vs. reality

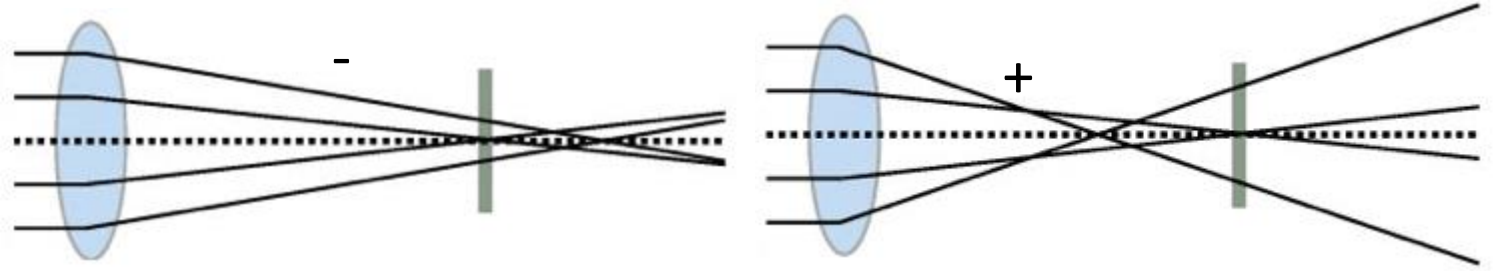


Chromatic aberration



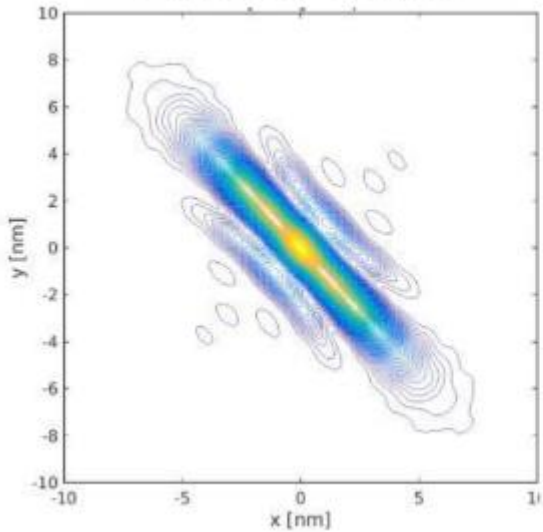
Abberations

Spherical aberration

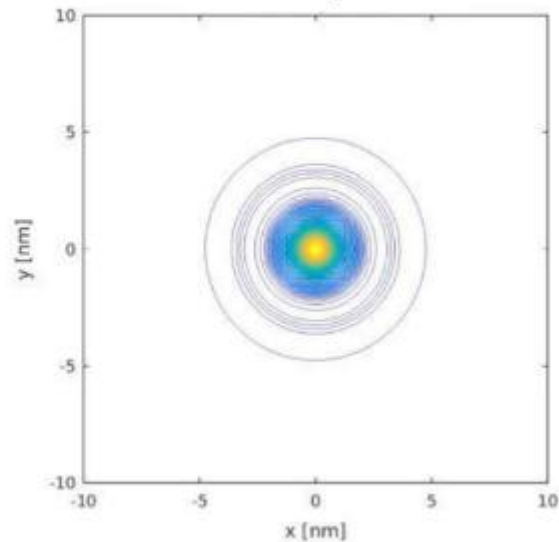


Astigmatism

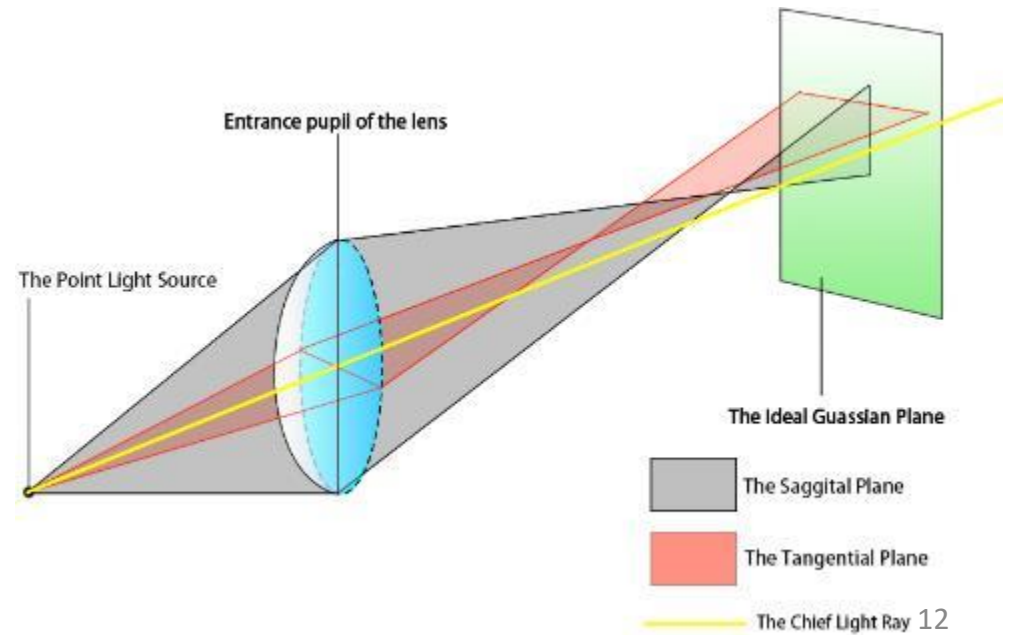
ellipticity 0.1 μm

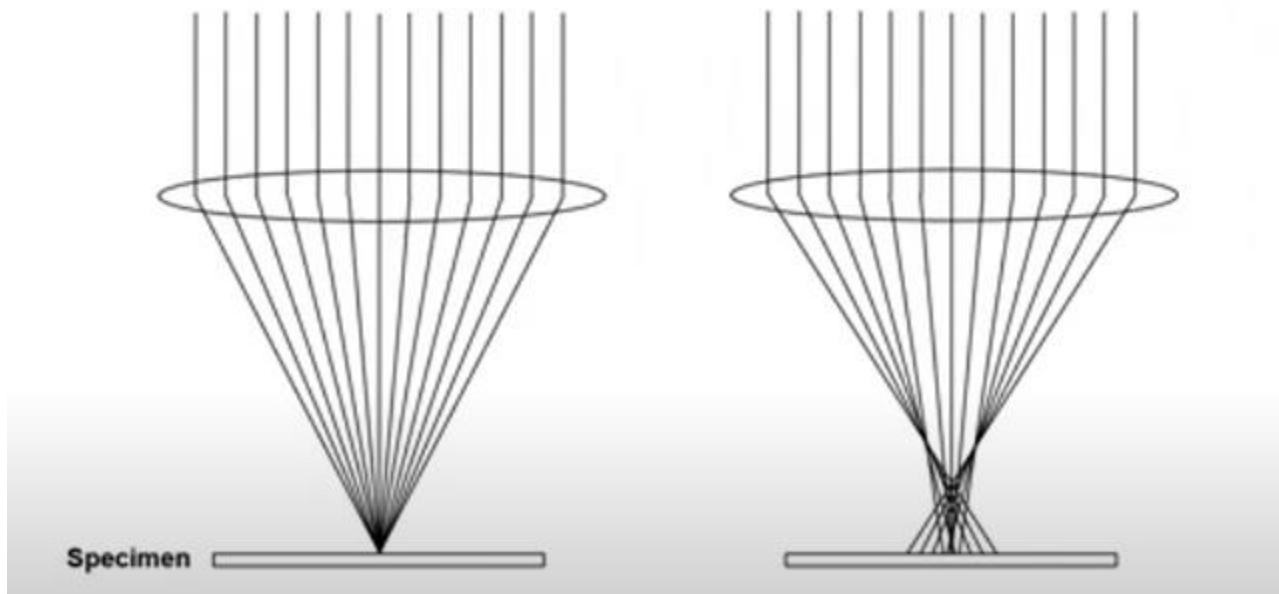


ideal system



Coma aberration





expectation

reality

$U=10\text{kV}$ (SEM) $\rightarrow \lambda = 0.01226 \text{ nm}$

$U=100\text{kV}$ (TEM) $\rightarrow \lambda = 0.0039 \text{ nm}$

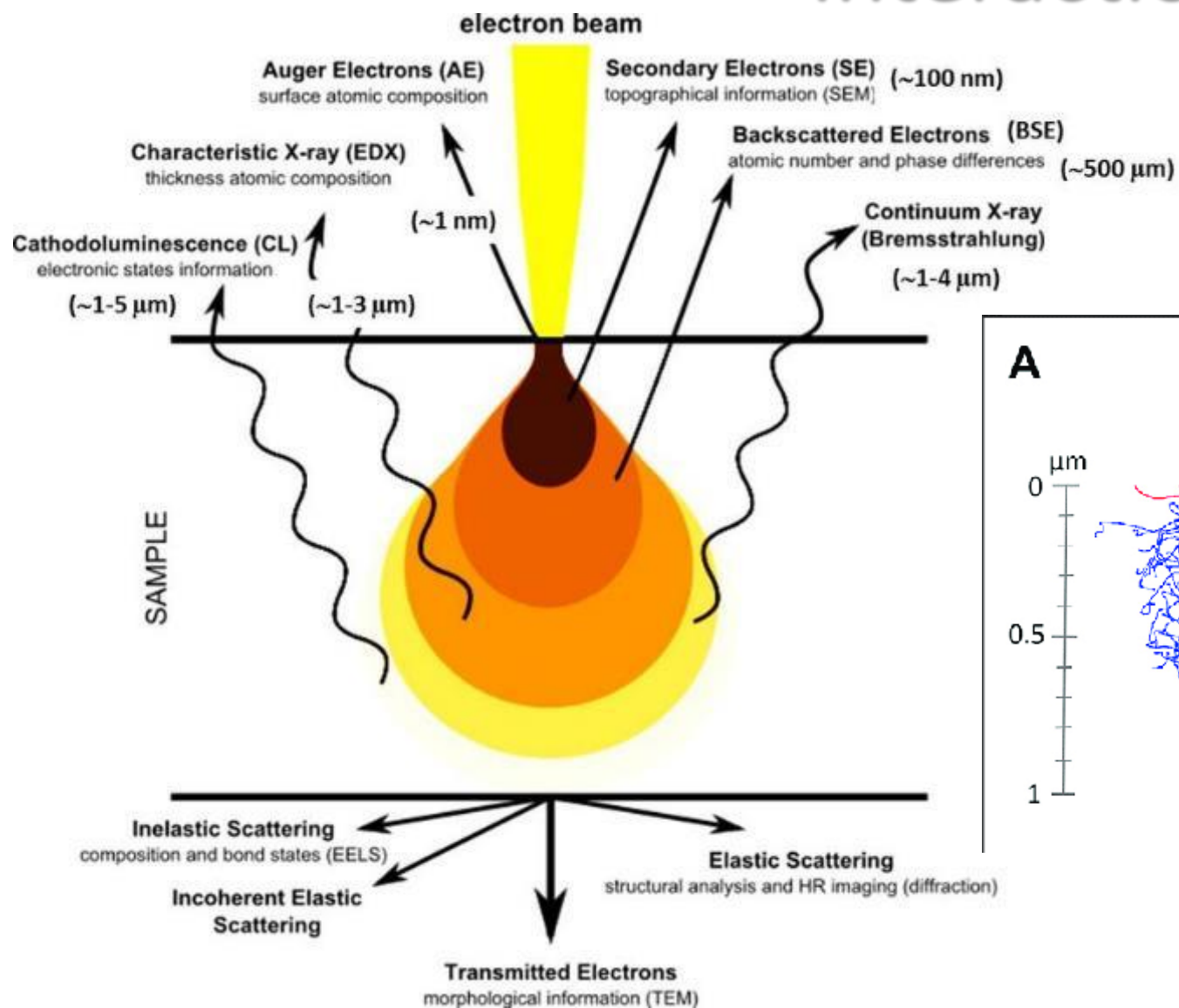
Visible light $\rightarrow \lambda = 390 - 760 \text{ nm}$

Typical SEM $\rightarrow d_d \sim 1 \text{ nm}$

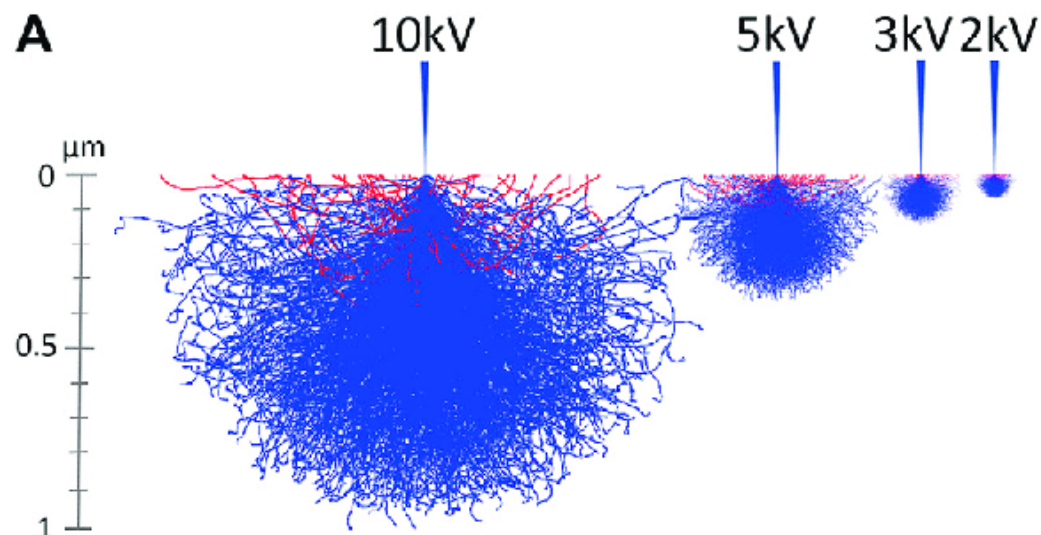
Typical TEM $\rightarrow d_d \sim 0.1 \text{ nm}$

High-end TEM (300 kV) $\rightarrow d_d \sim 0.05 \text{ nm}$

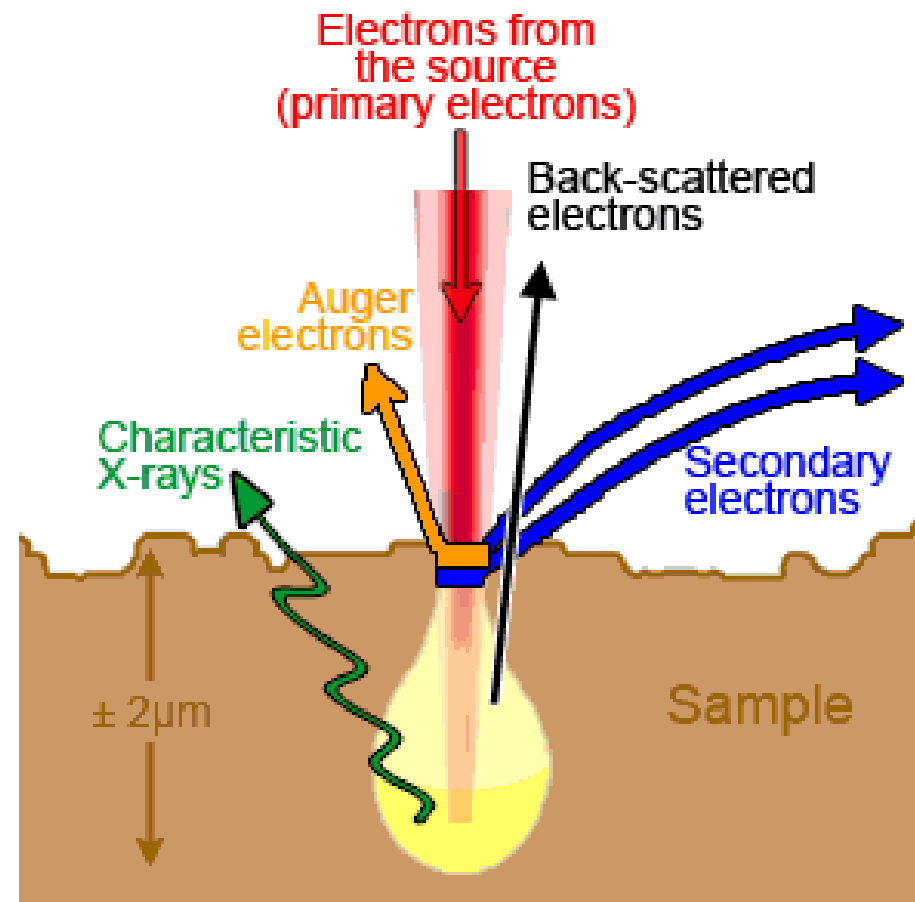
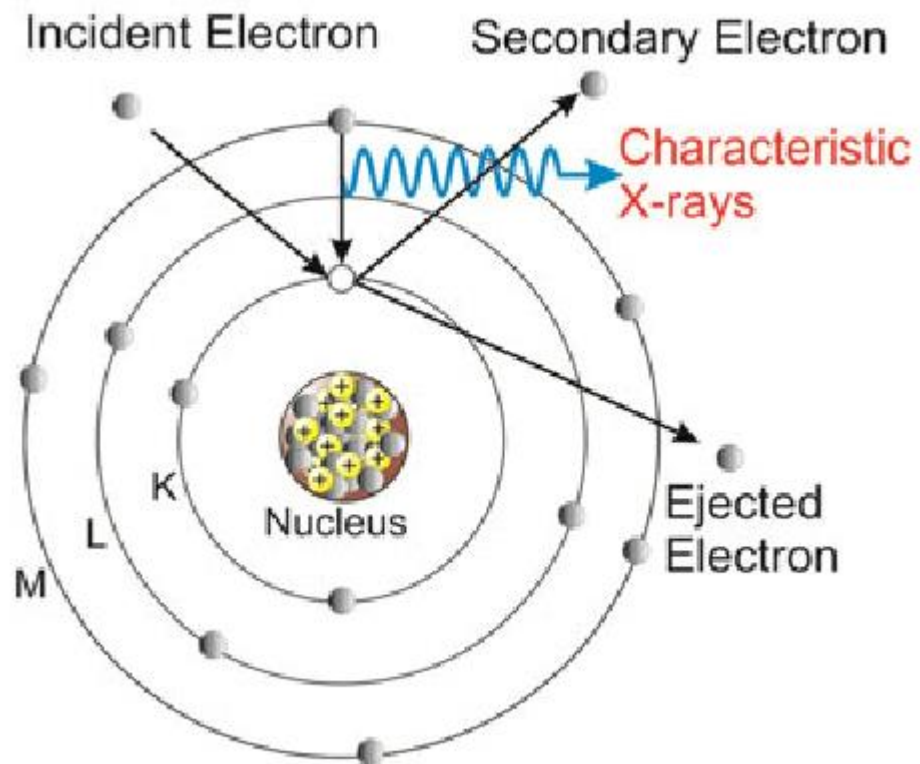
Interactions



A



Interactions





Primary

SE

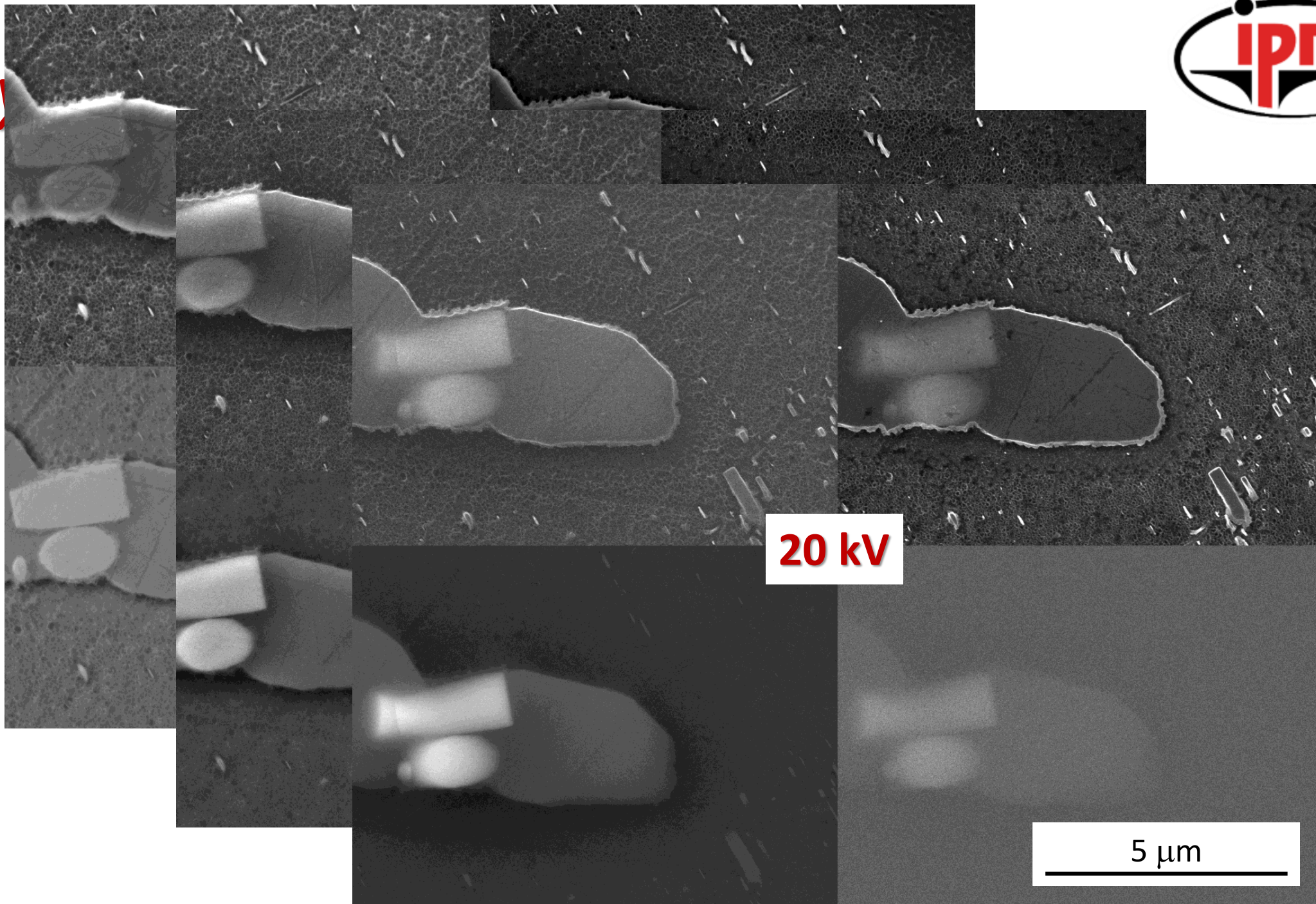
Everhart-
Thornley SE

In – lens SE

BSE

BSE

BSE



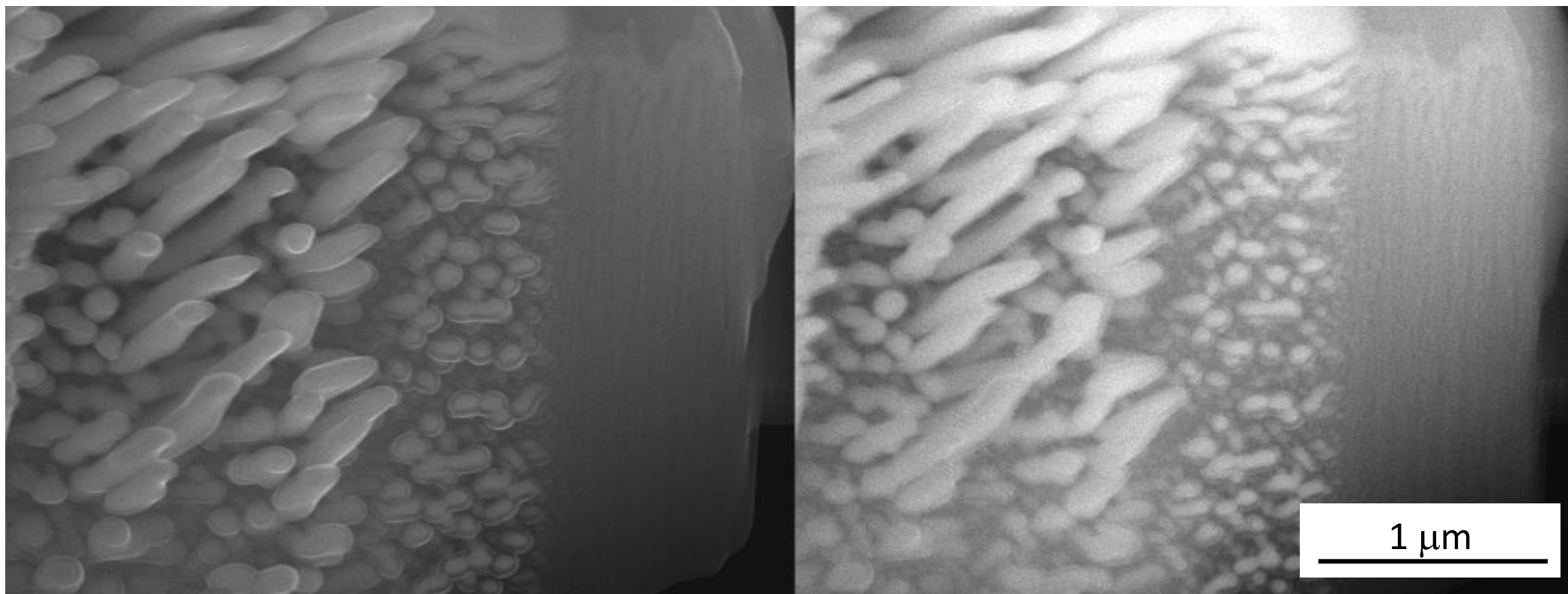
20 kV

5 μm

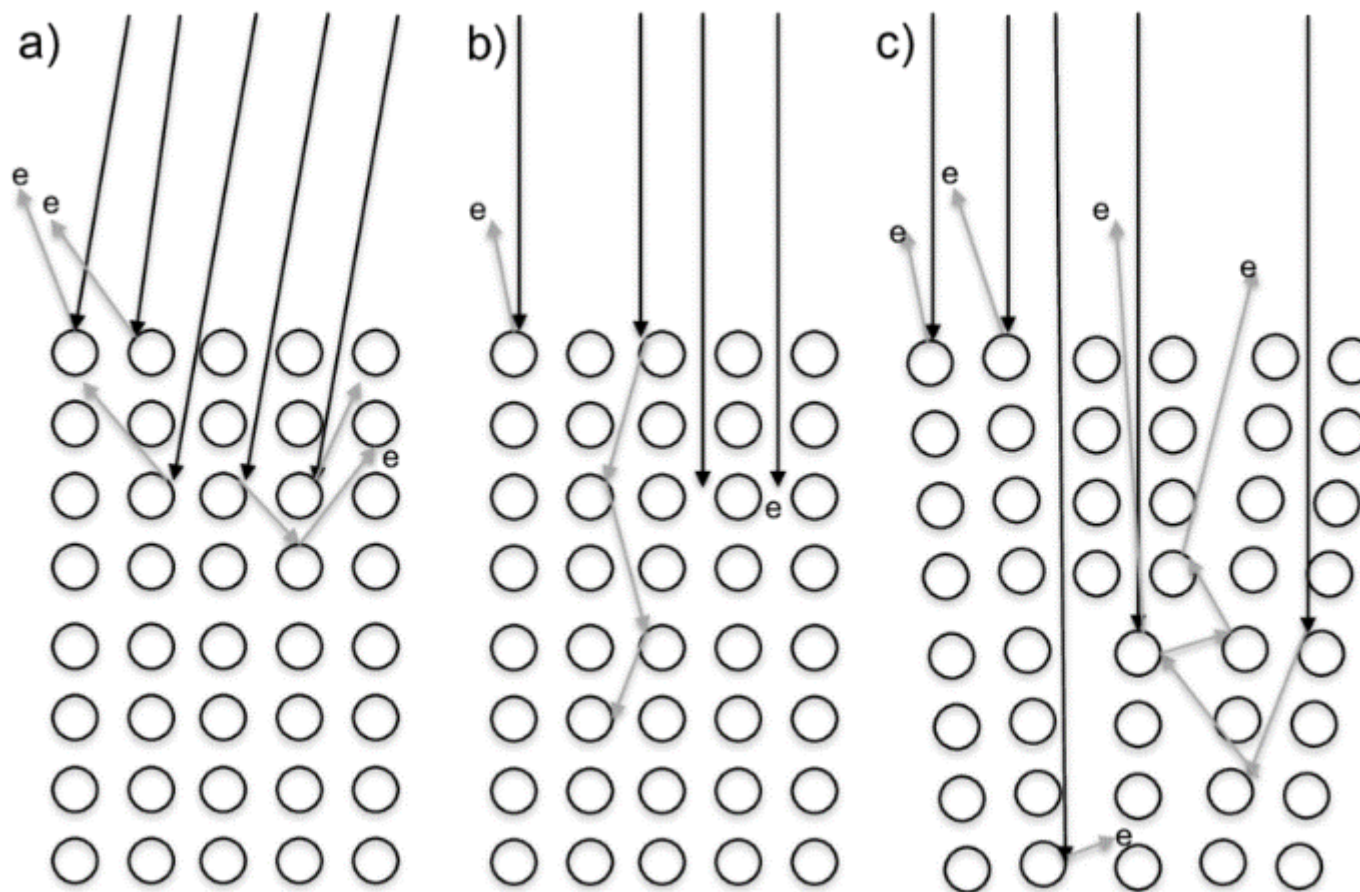
Secondary electrons

In – lens SE

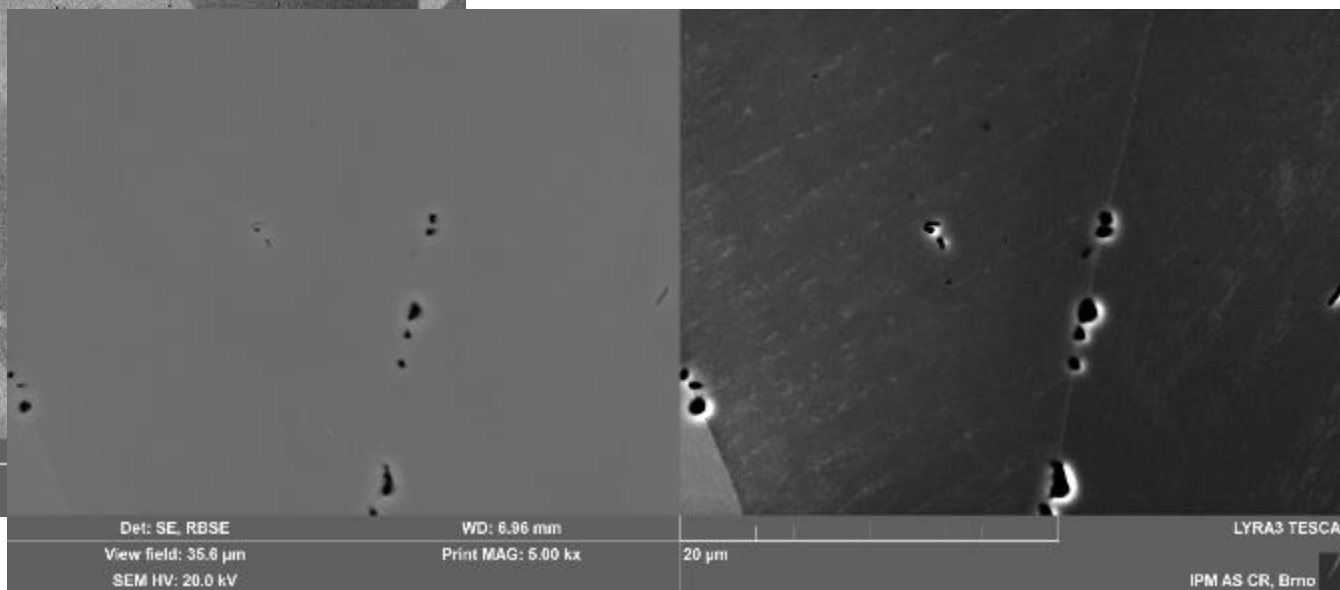
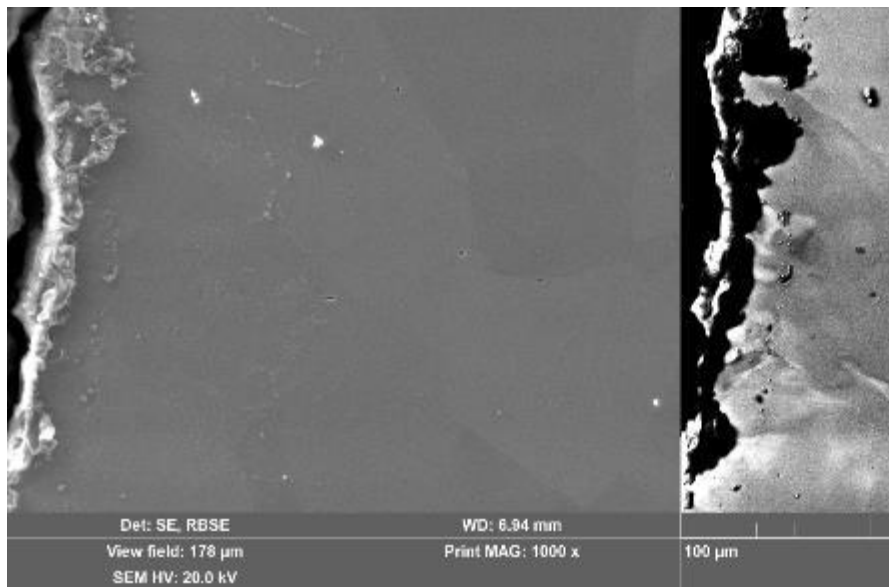
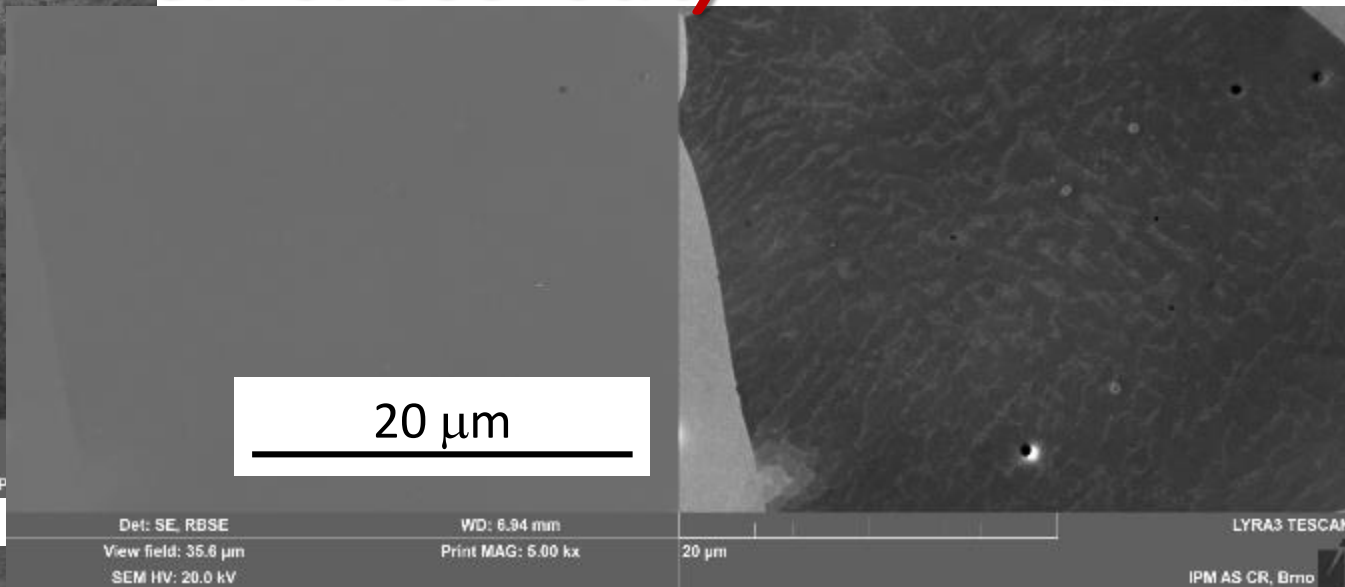
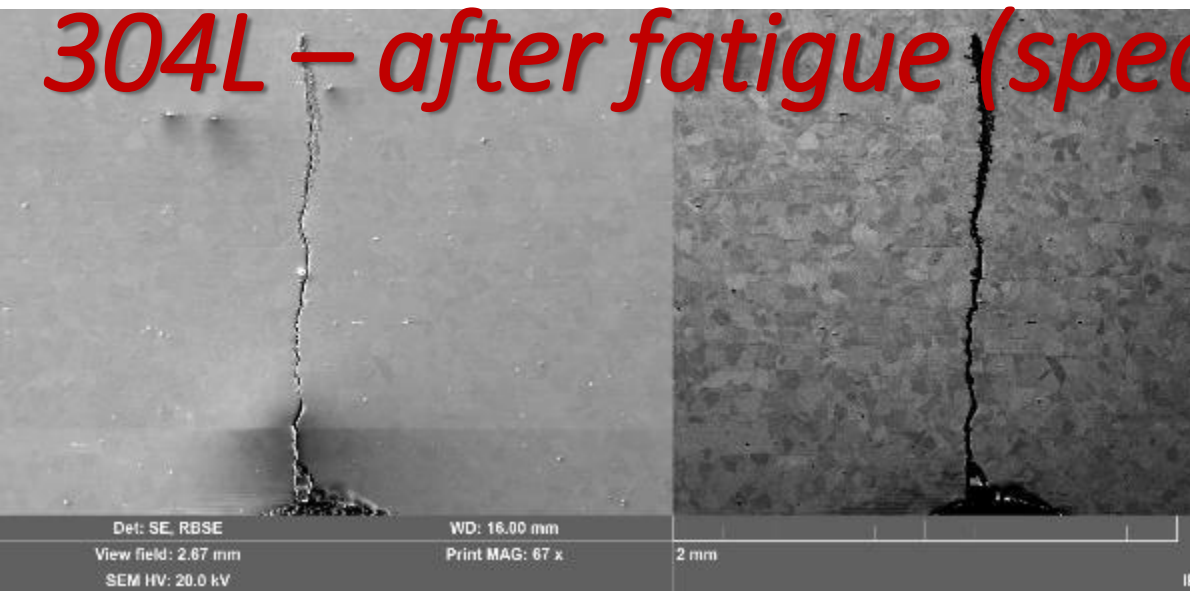
Everhart-Thornley SE

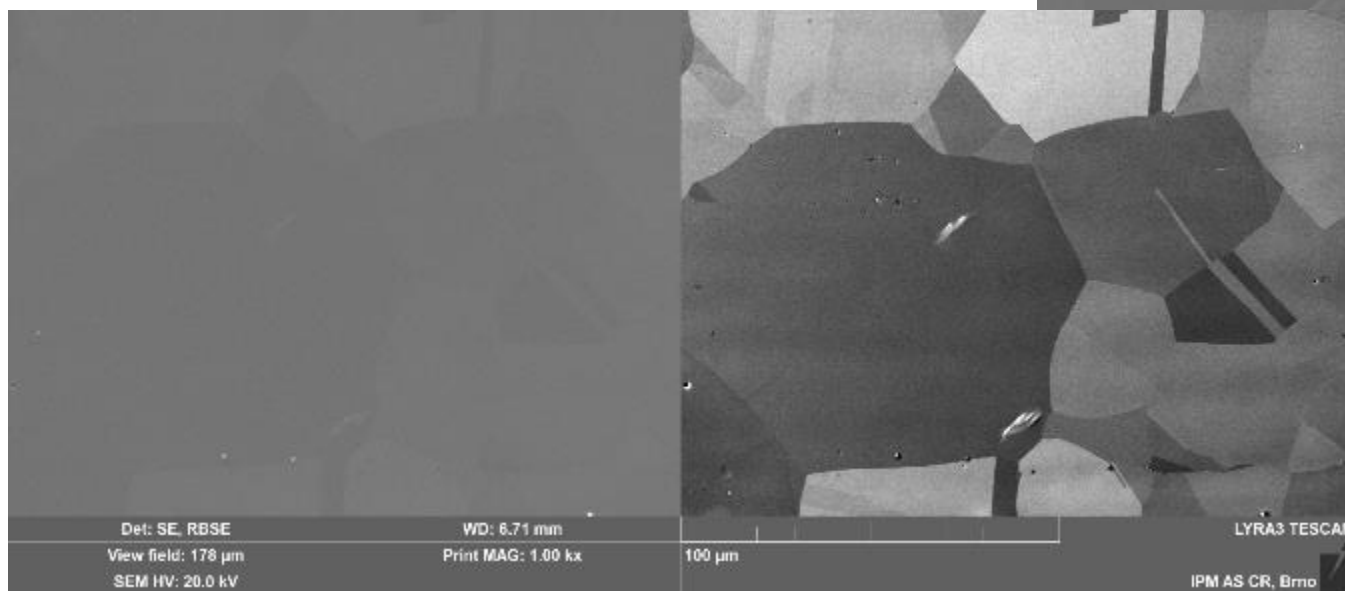
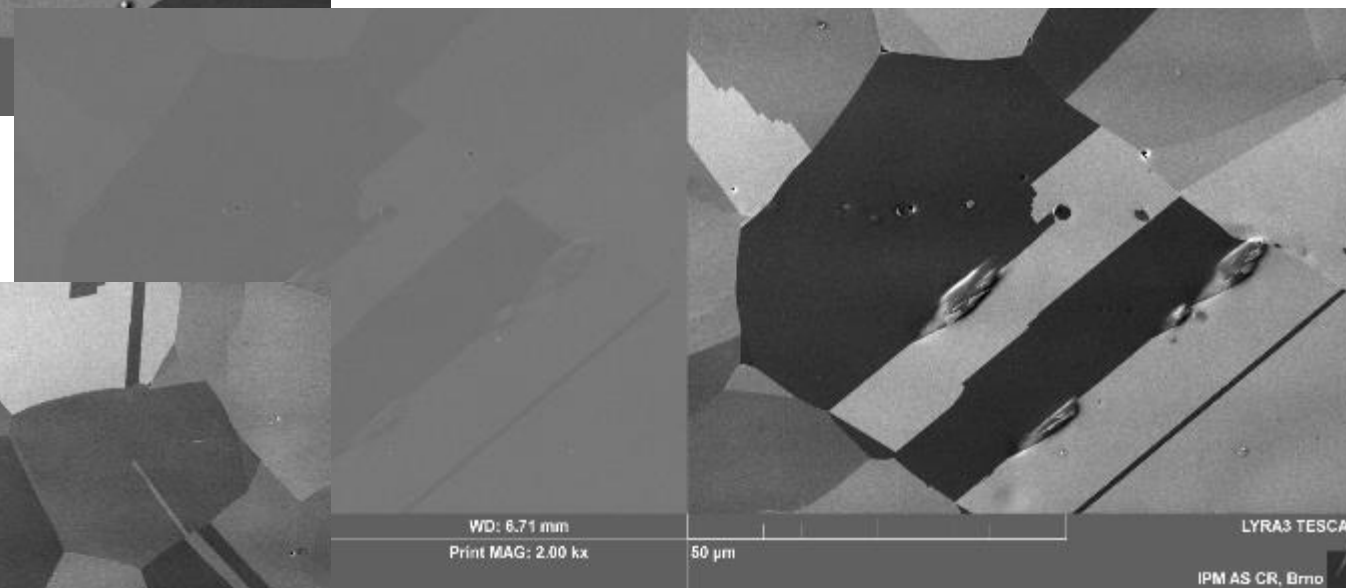
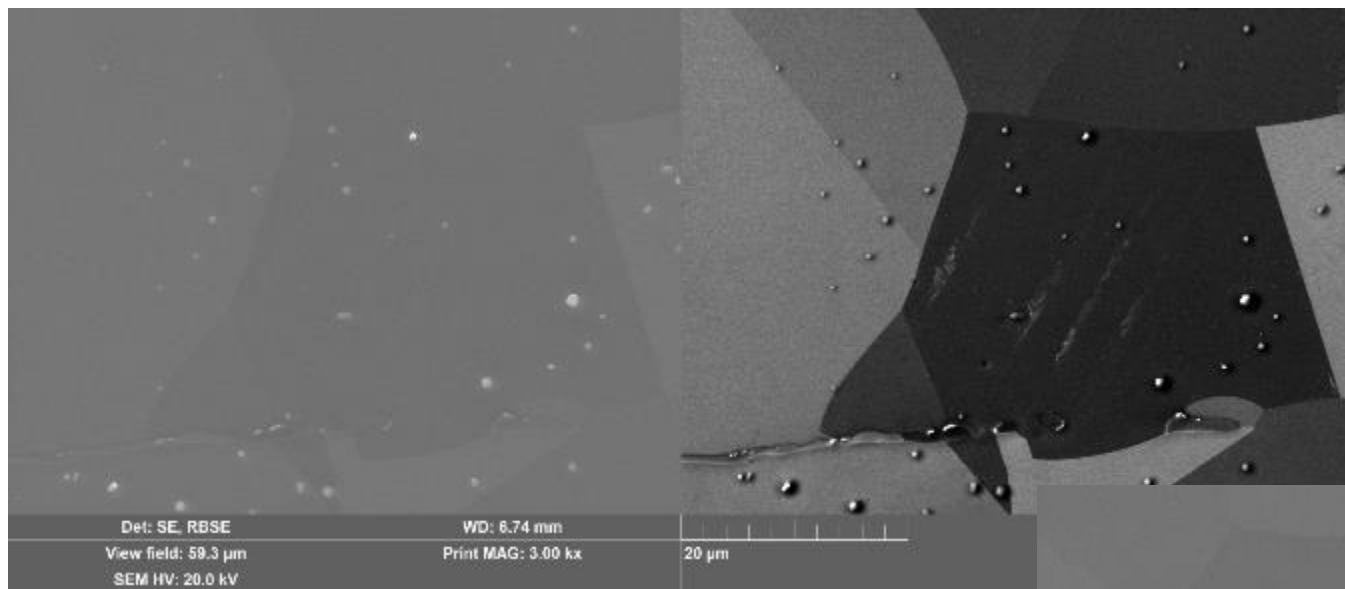


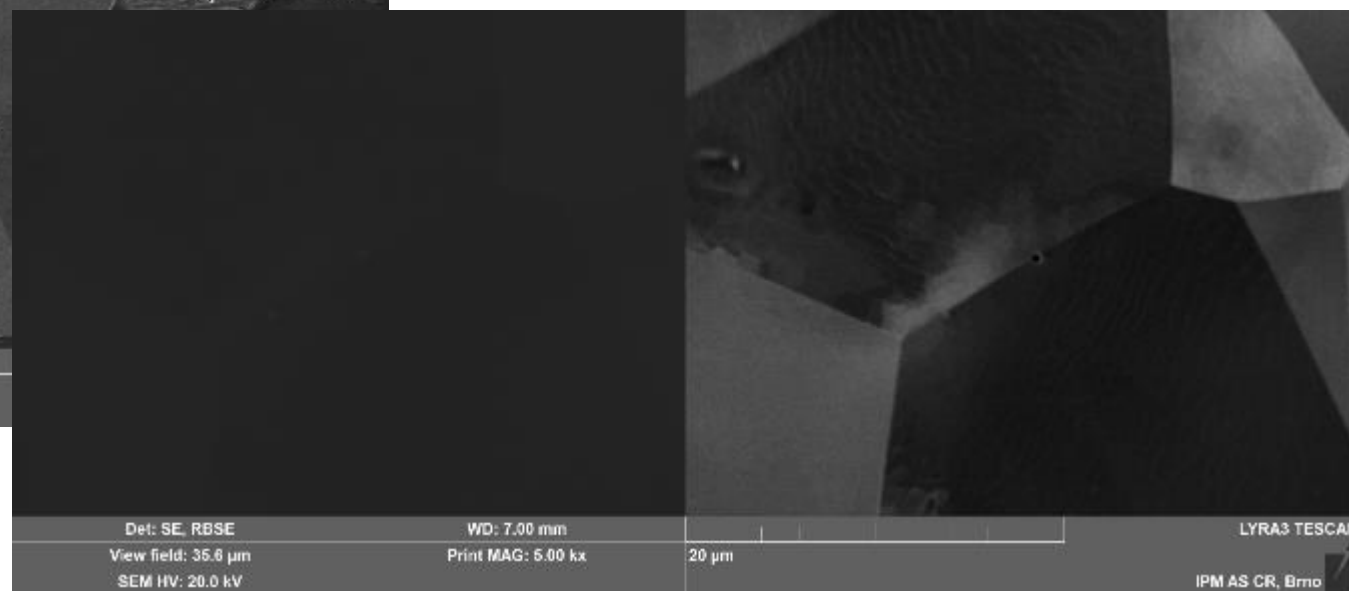
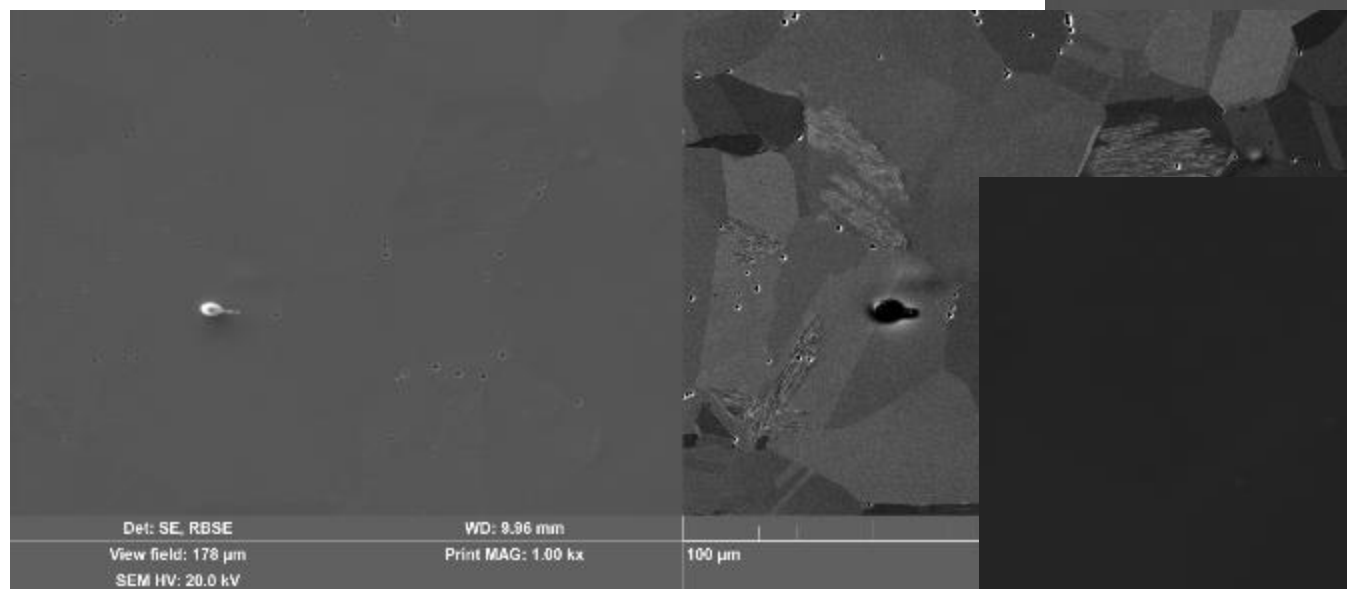
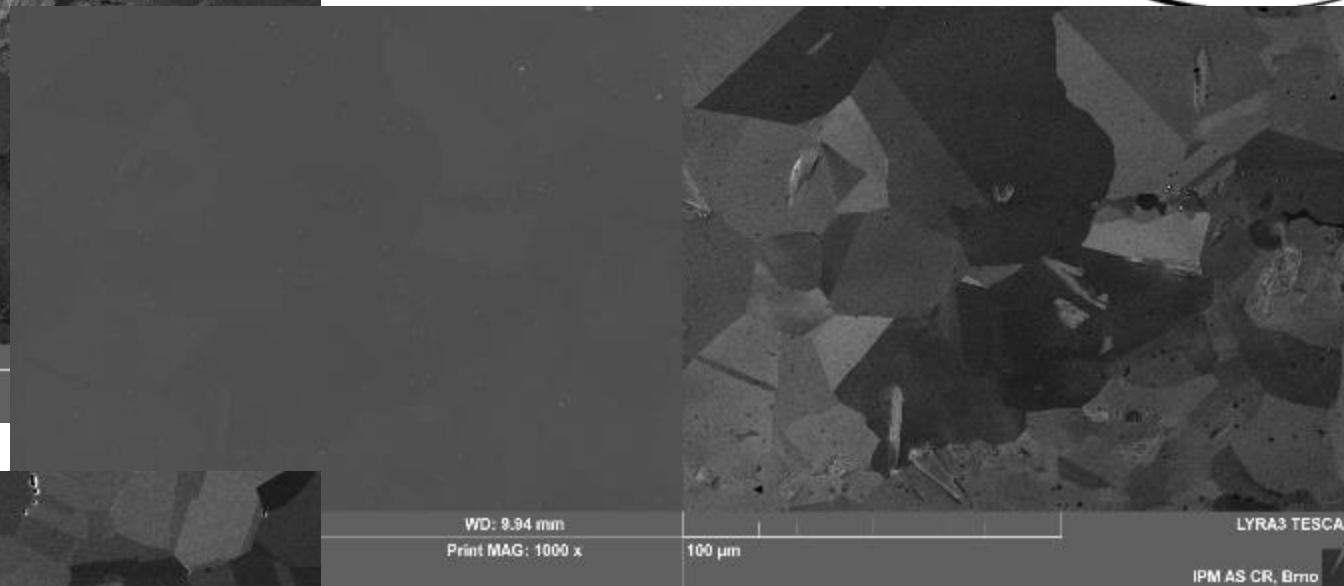
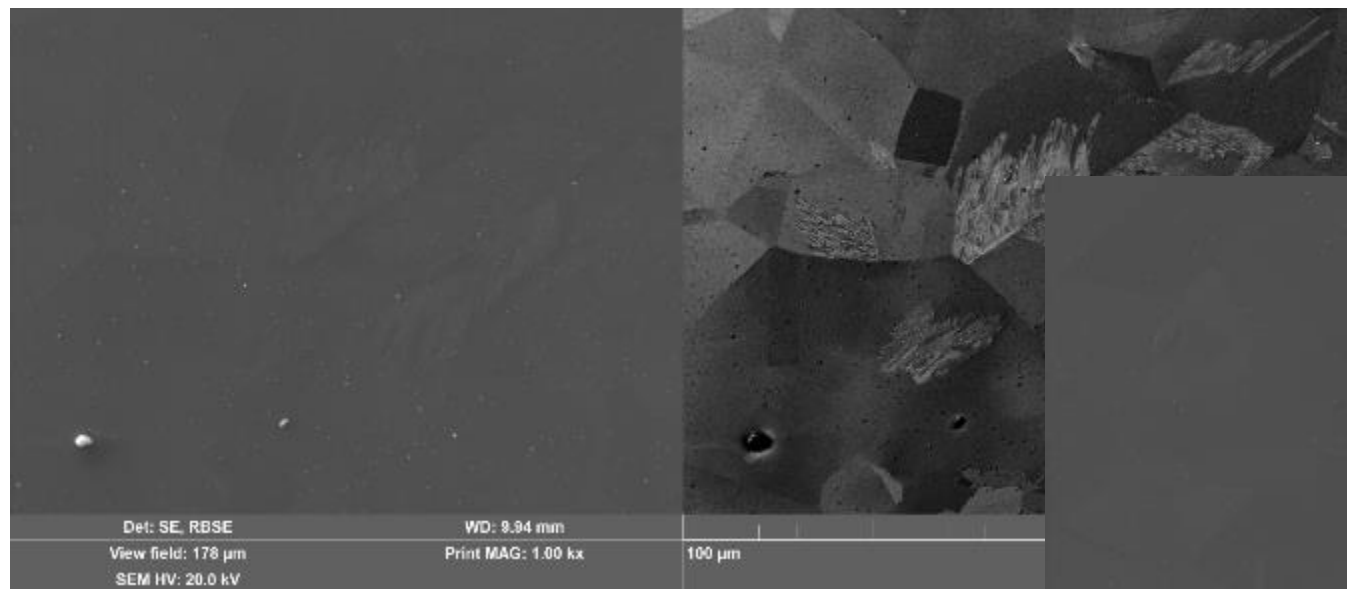
ECCI – Electron channeling contrast imaging



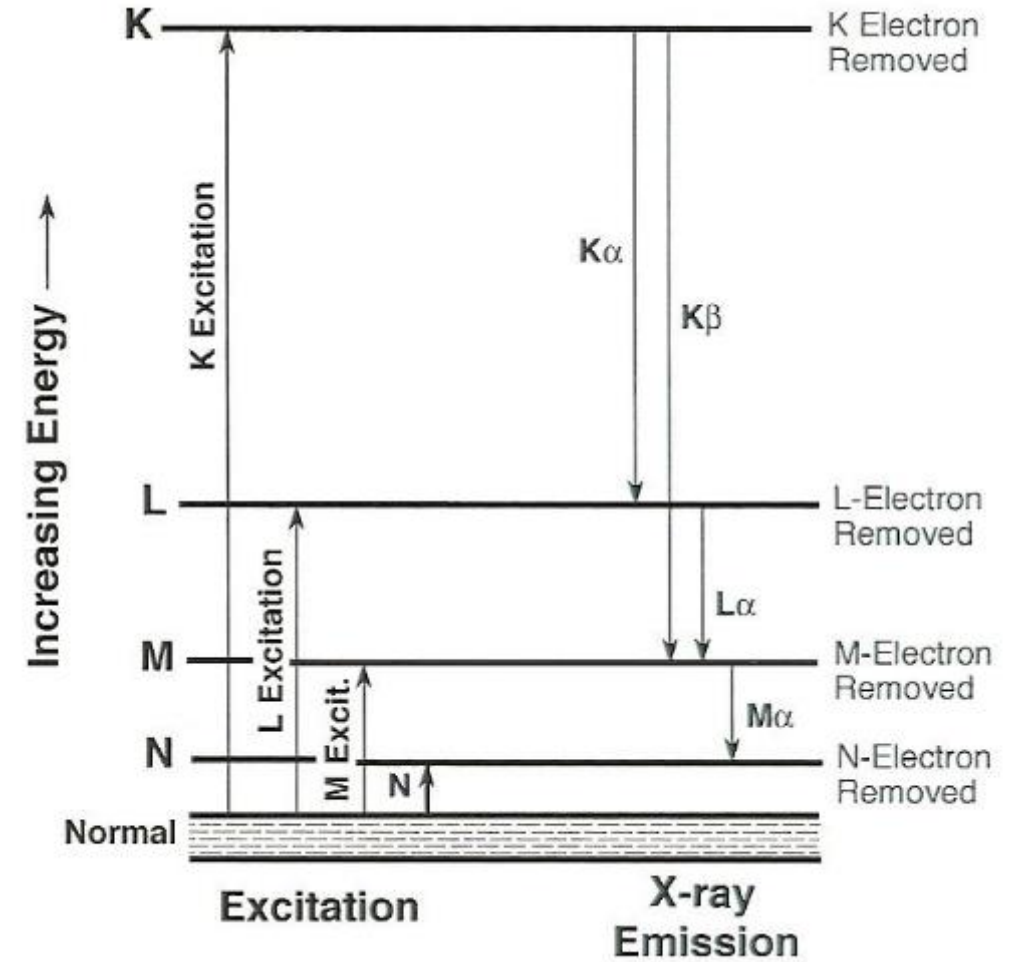
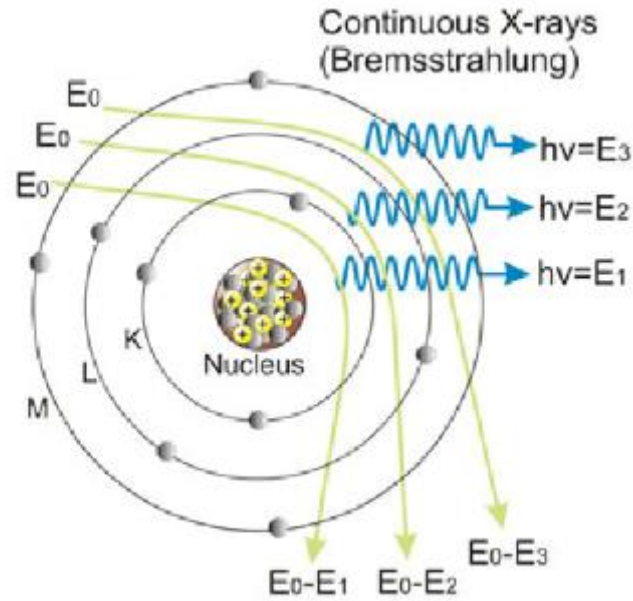
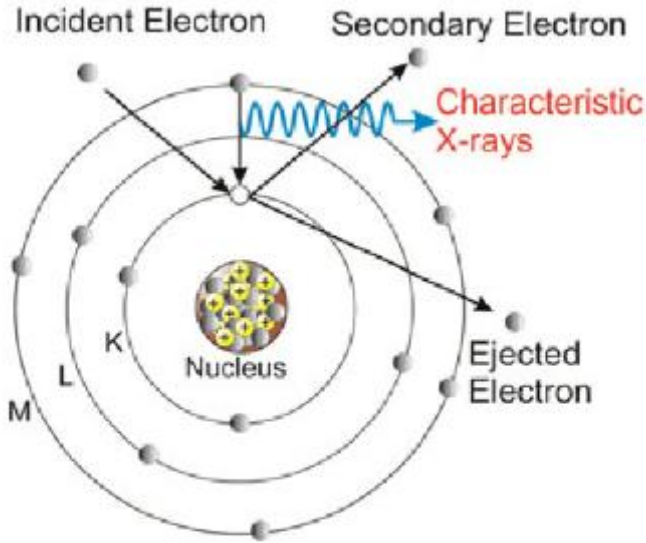
304L – after fatigue (specimen cross-cut)



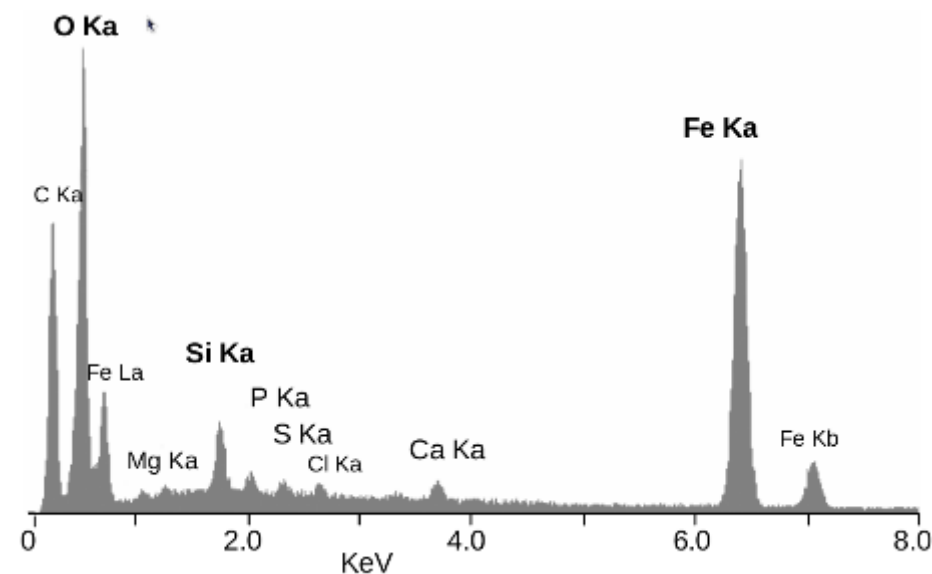
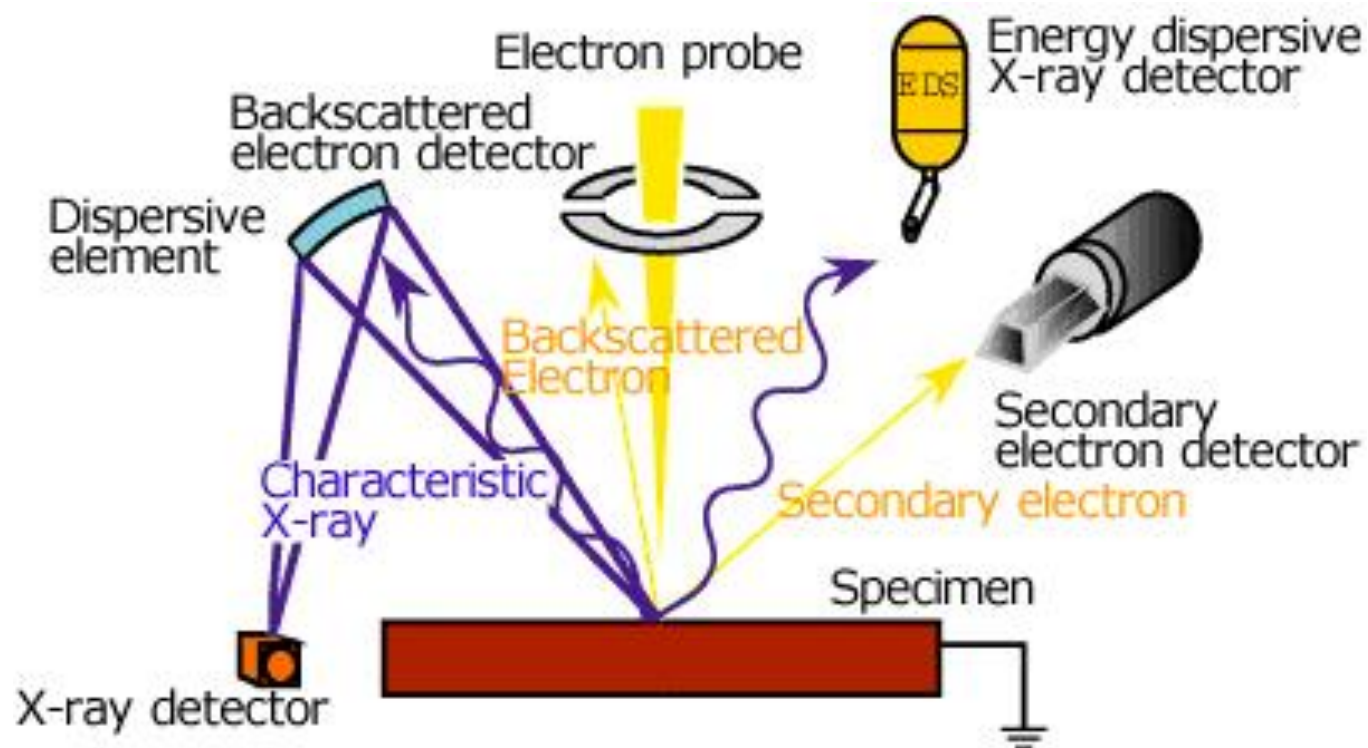




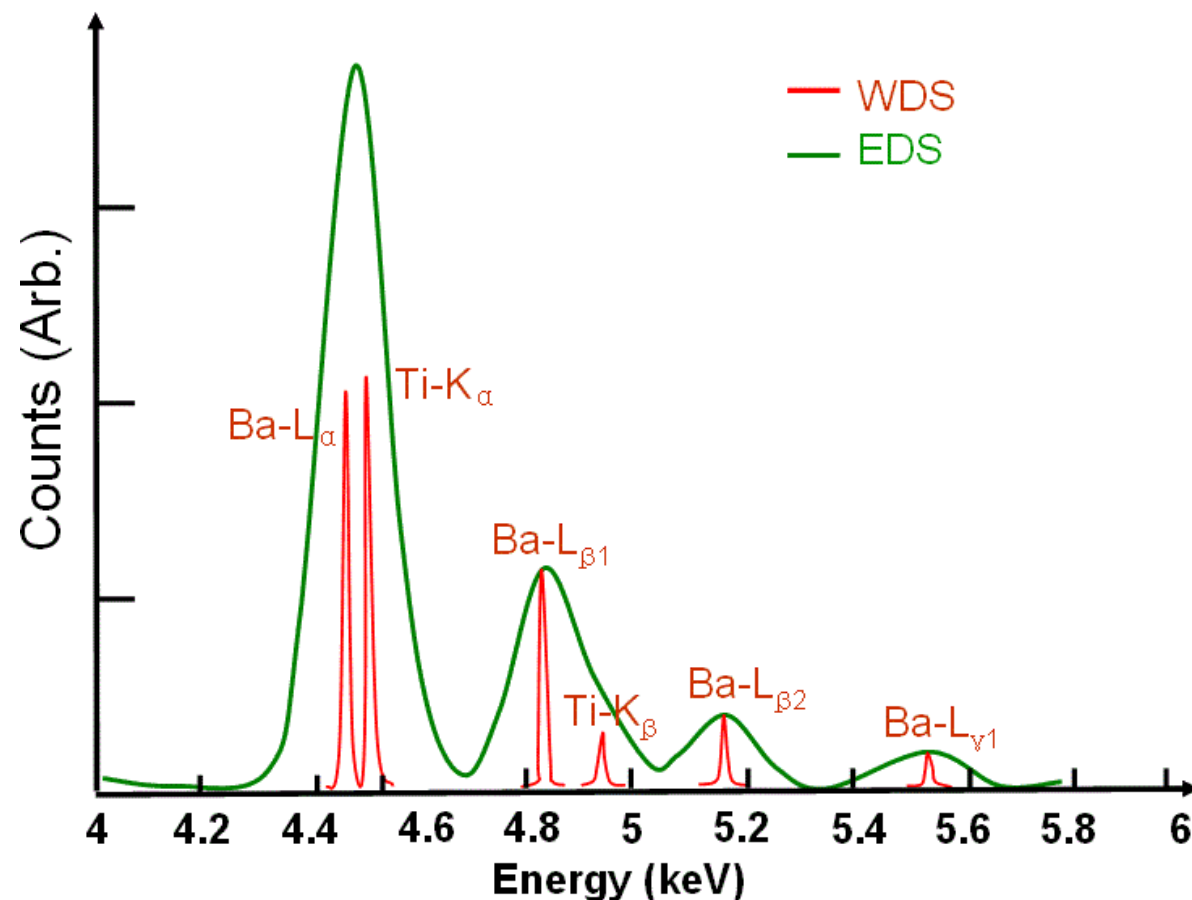
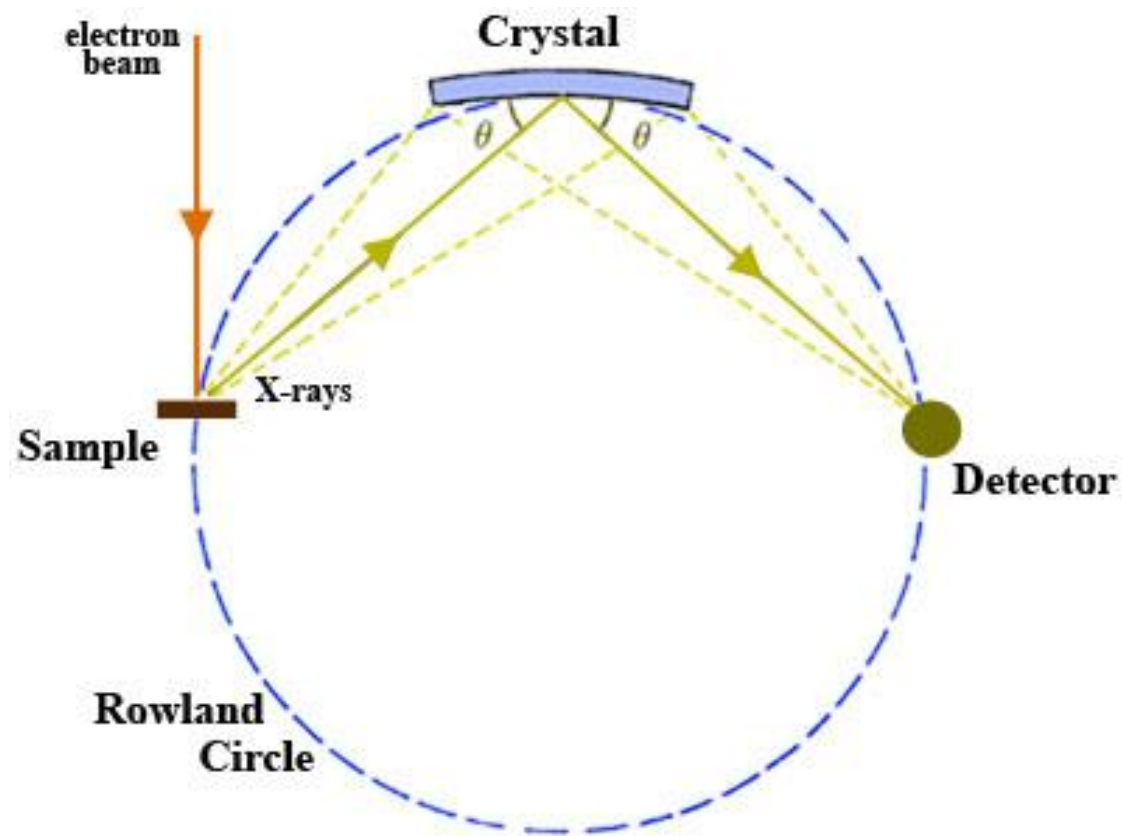
Energy and wave dispersive spectroscopy

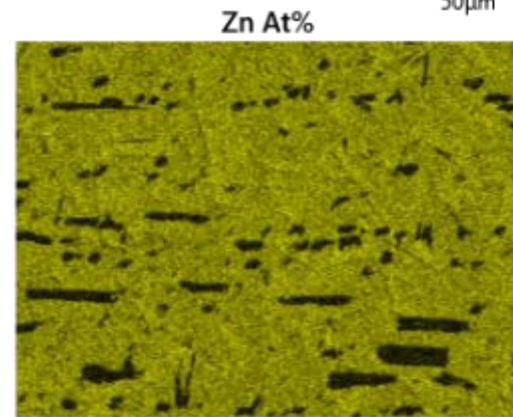
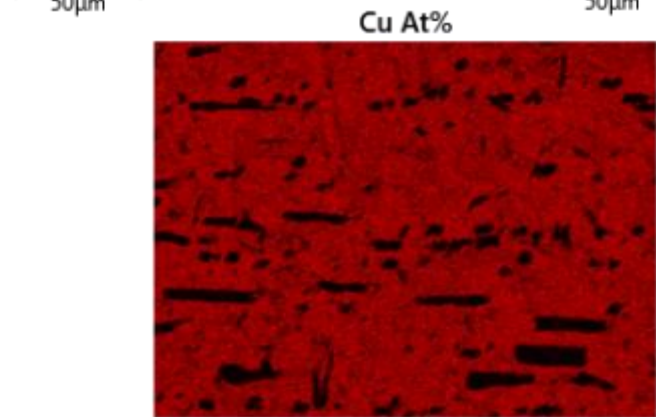
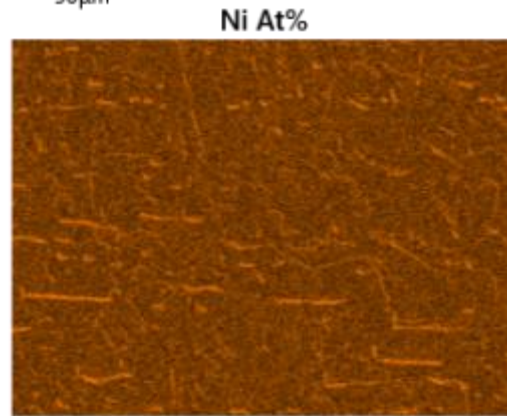
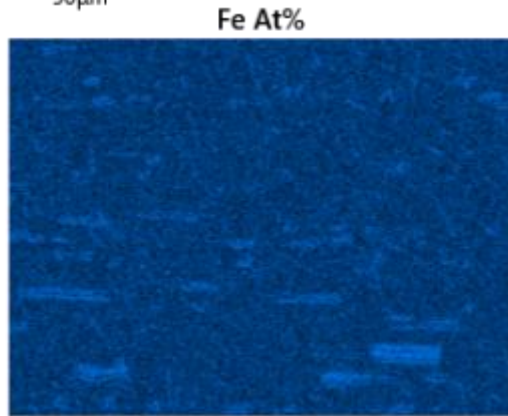
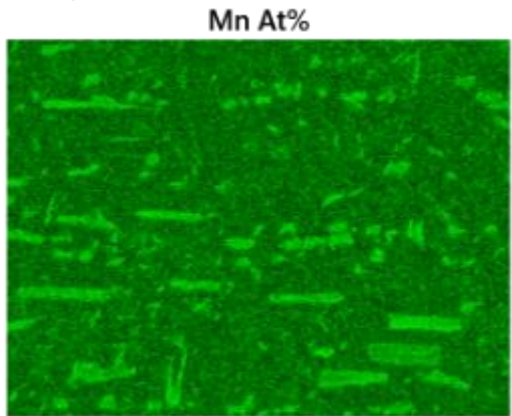
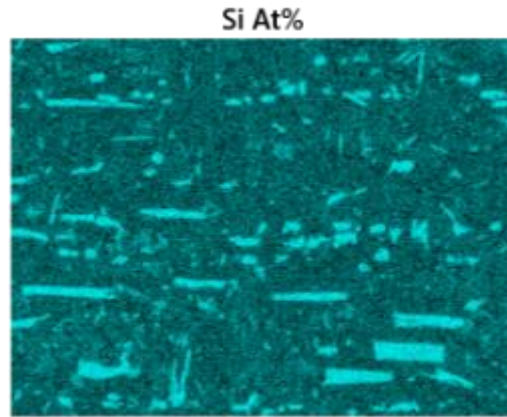
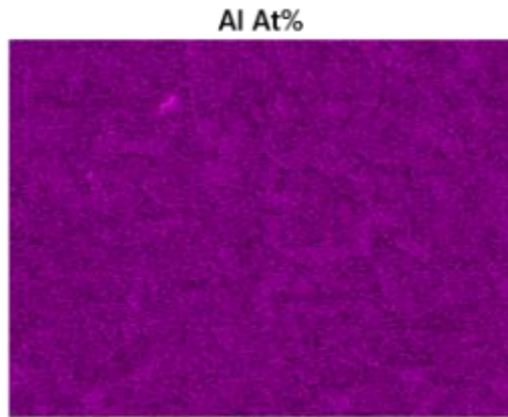
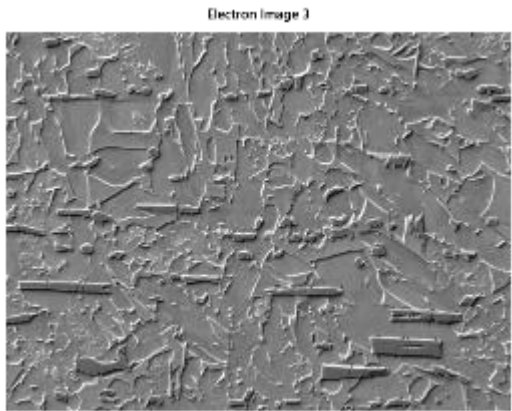


Energy dispersive spectroscopy - EDS



Wave dispersive spectroscopy - WDS

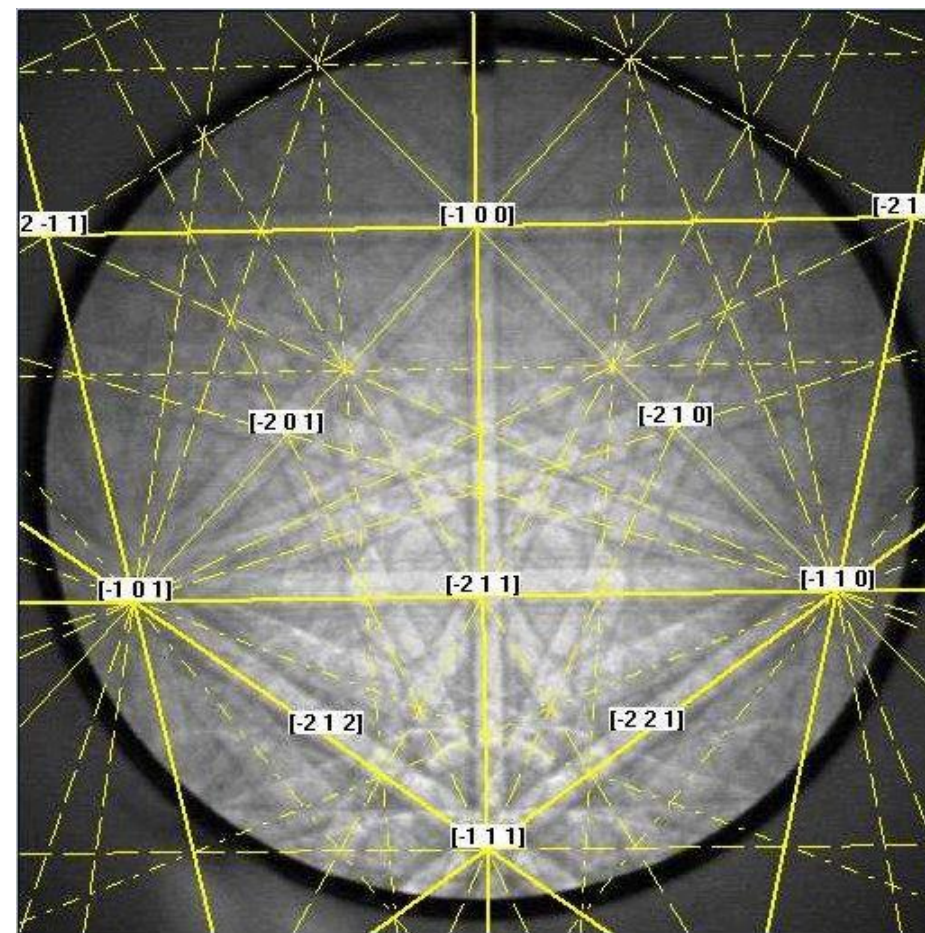
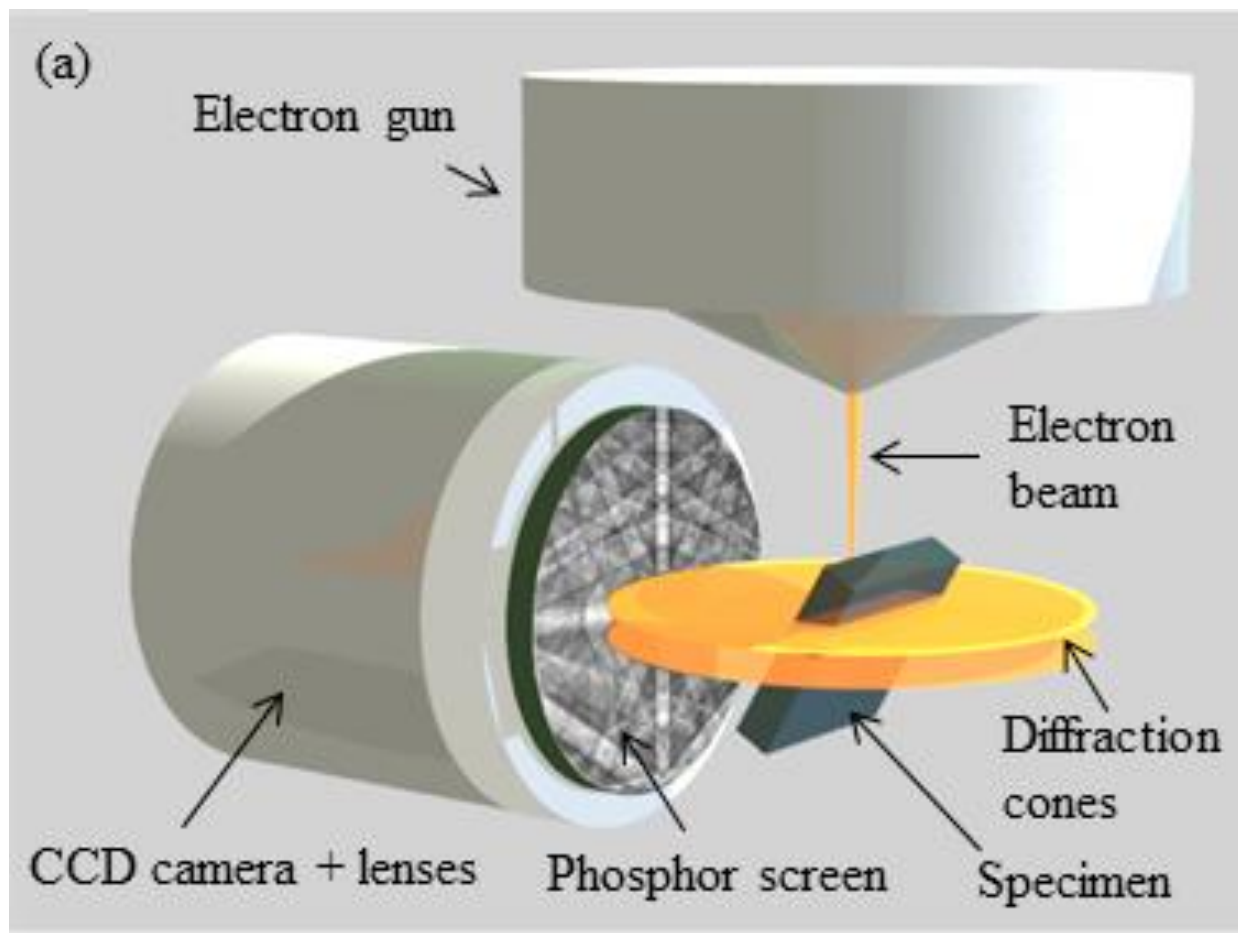




element	wt. %
Cu	60.1
Zn	27.5
Mn	6.5
Si	2.6
Al	1.3
Ni	1.1
Fe	1.0

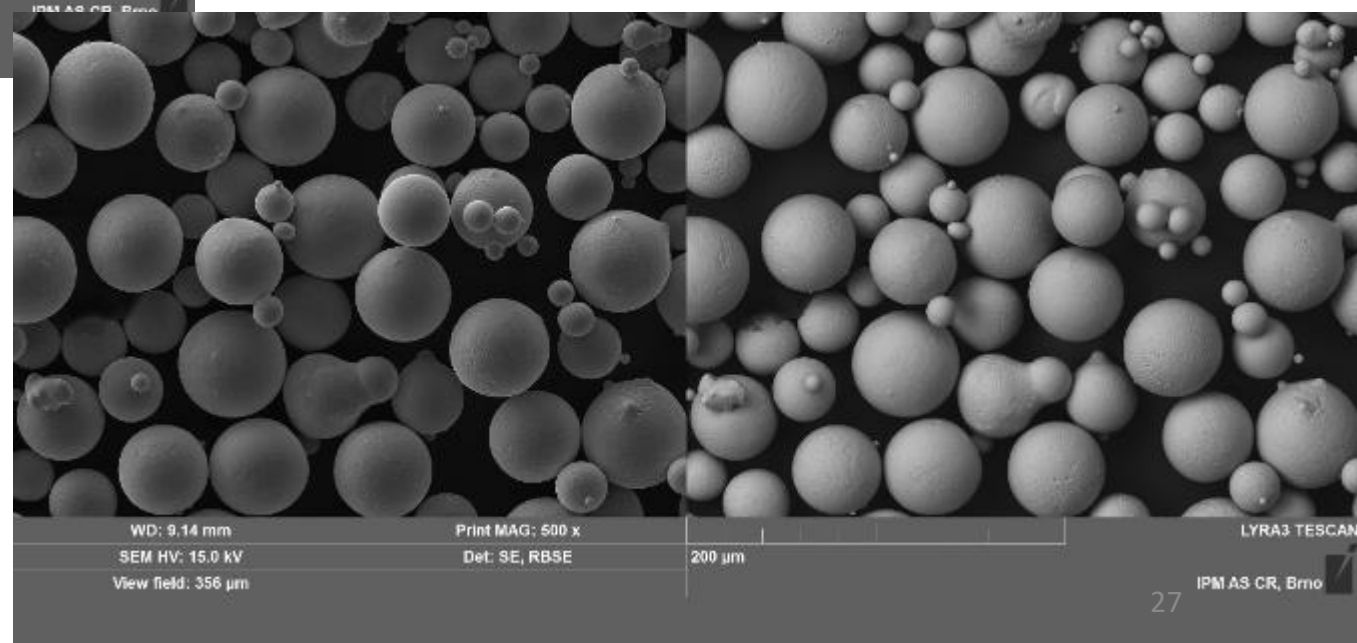
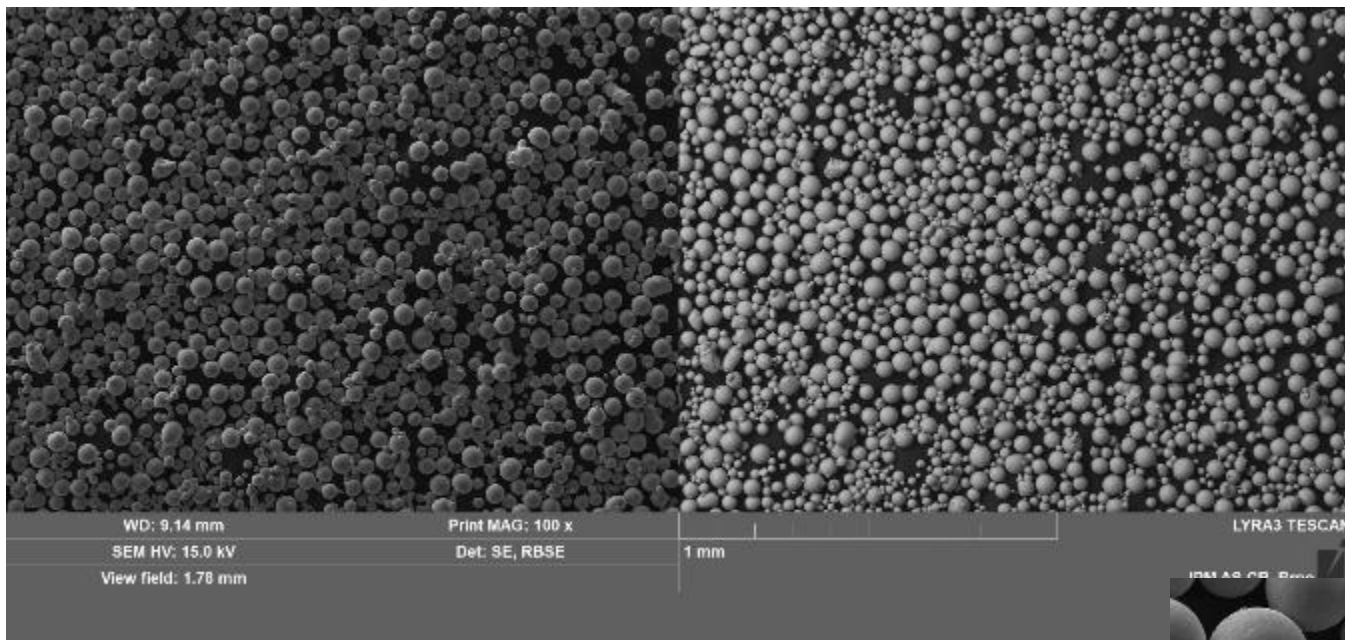
lead-free brass

Electron backscattered diffraction - EBSD

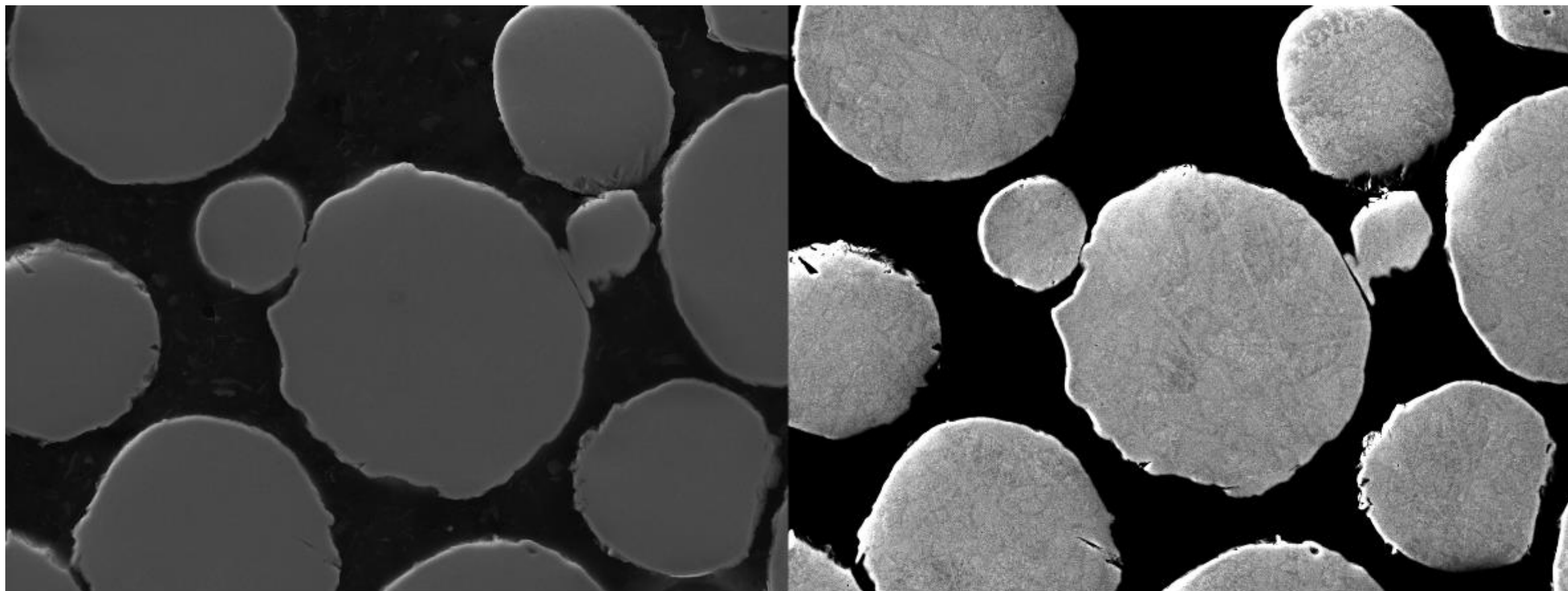


crystallographic information, crystal orientation

Examples



Examples



Det: SE, RBSE

View field: 100.0 μm

SEM HV: 20.0 kV

WD: 8.96 mm

Print MAG: 1.78 kx

Date(m/d/y): 09/14/22

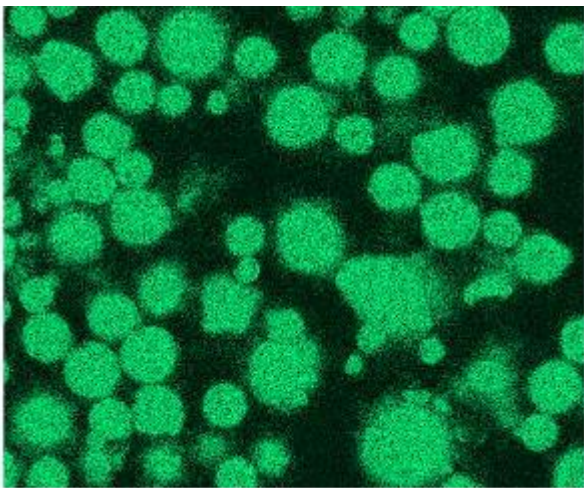
50 μm

LYRA3 TESCAN

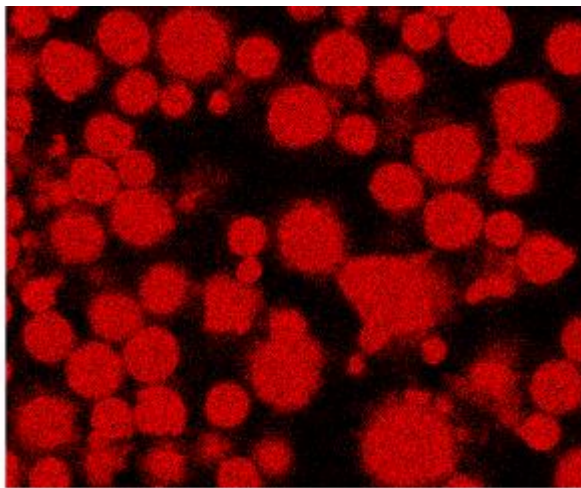
IPM AS CR, Brno

Examples

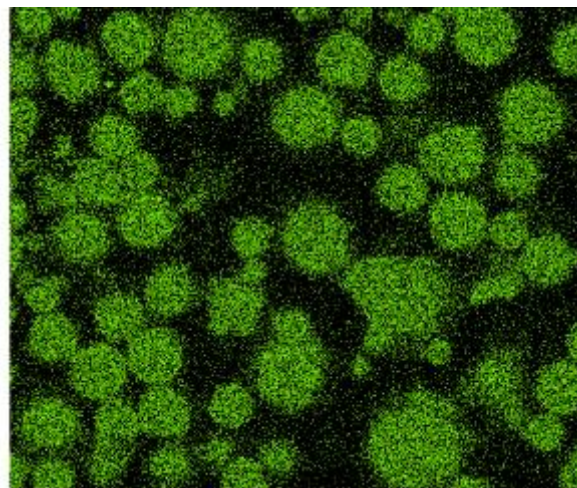
Ni



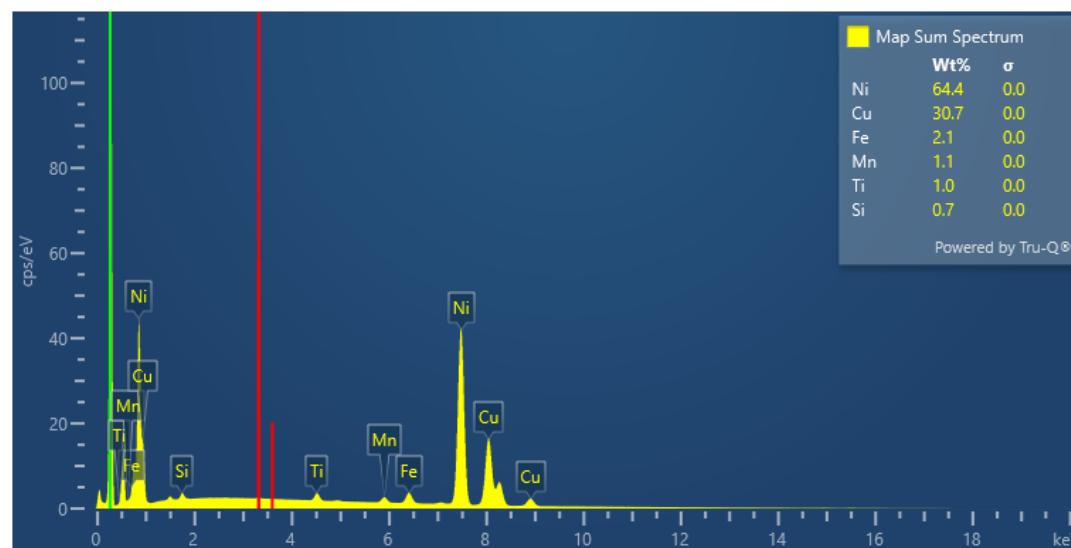
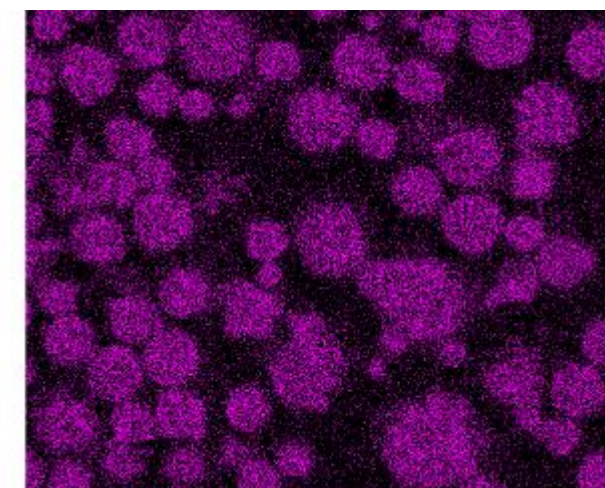
Cu



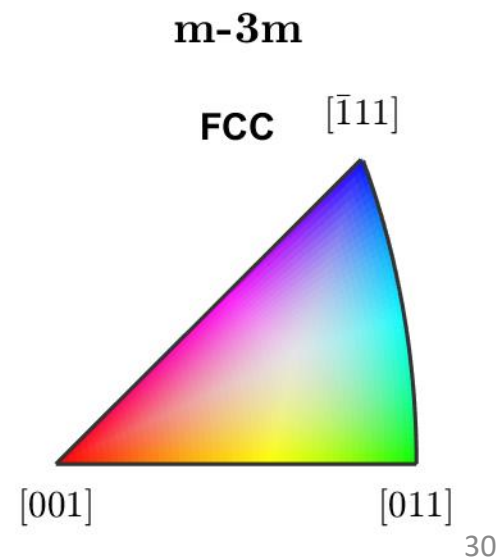
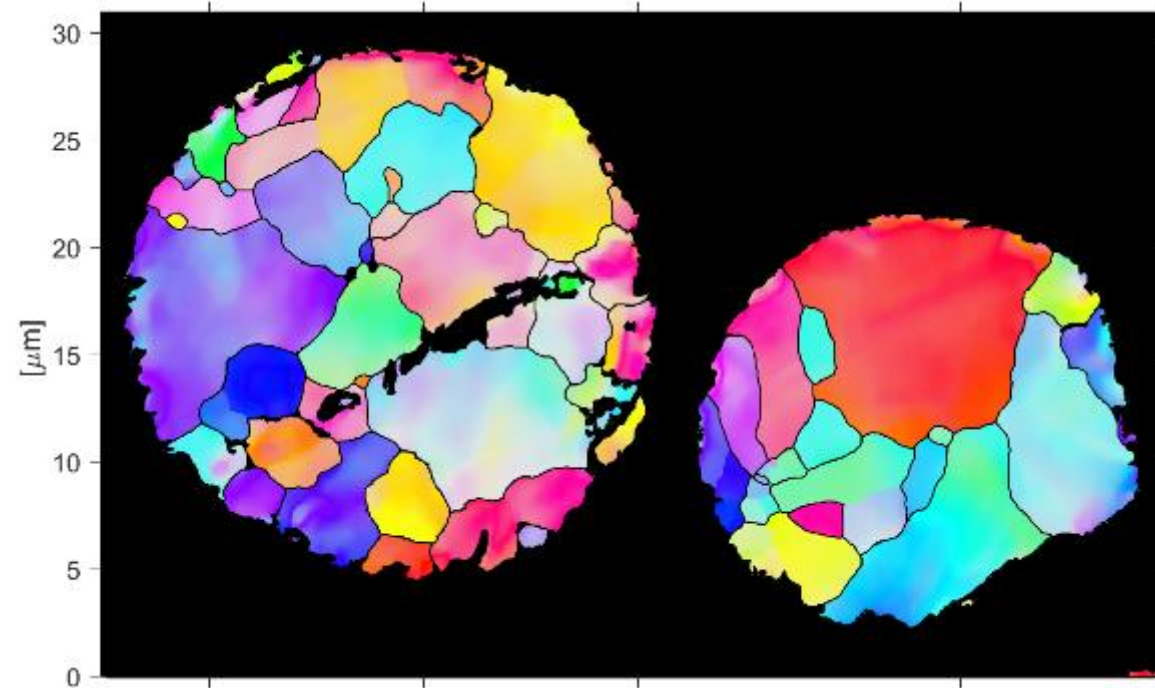
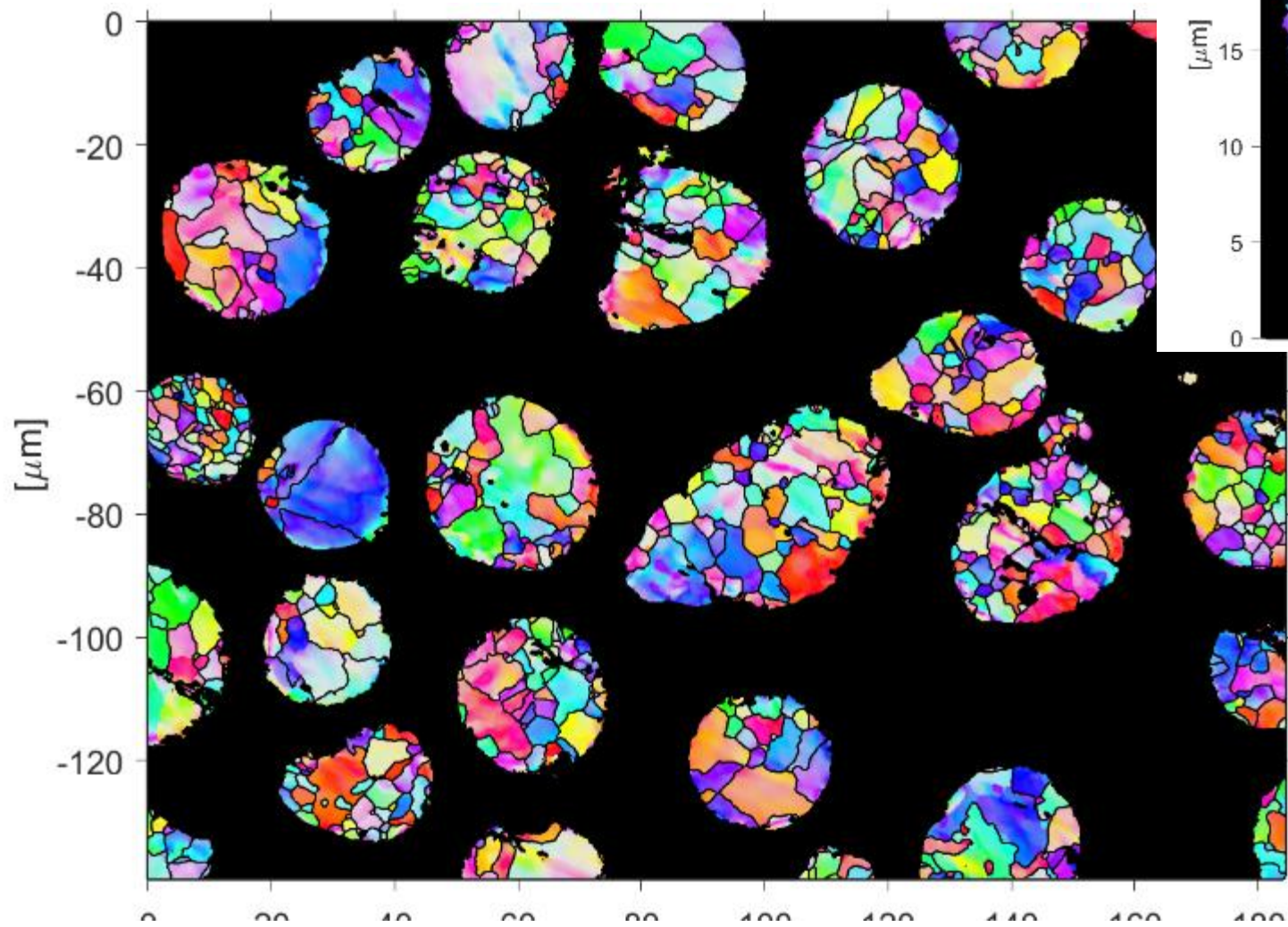
Fe



Ti



Examples



Examples



SEM HV: 10.0 kV

View field: 356 μm

WD: 9.50 mm

Det: SE, BSE

Print MAG: 500 x

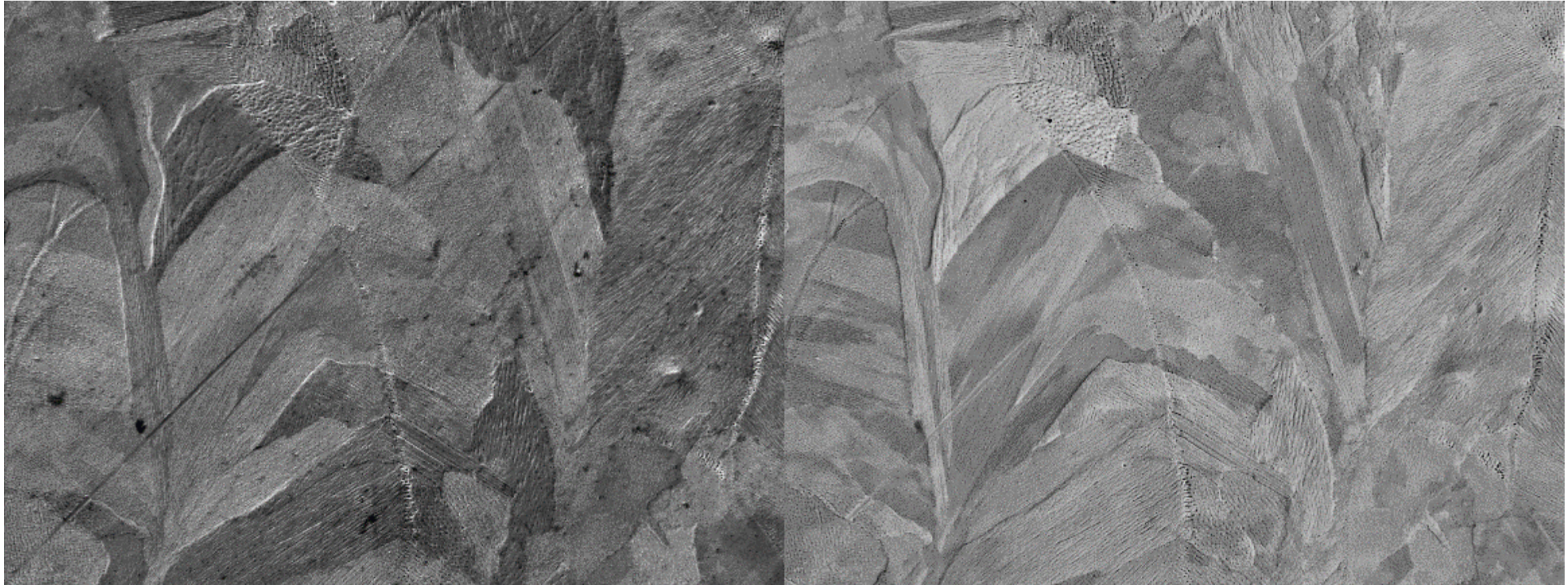
Date(m/d/y): 05/27/22

200 μm

LYRA3 TESCAN



Examples



SEM HV: 10.0 kV

Det: SE, BSE

View field: 71.2 μm

Print MAG: 2.50 kx

50 μm

WD: 9.46 mm

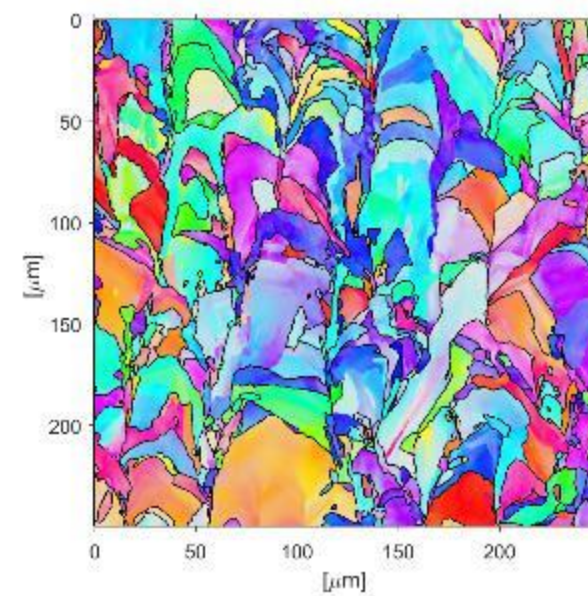
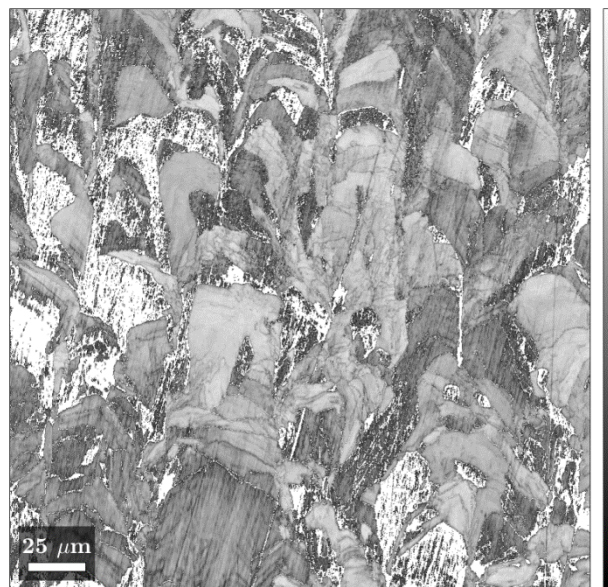
Date(m/d/y): 05/27/22

LYRA3 TESCAN

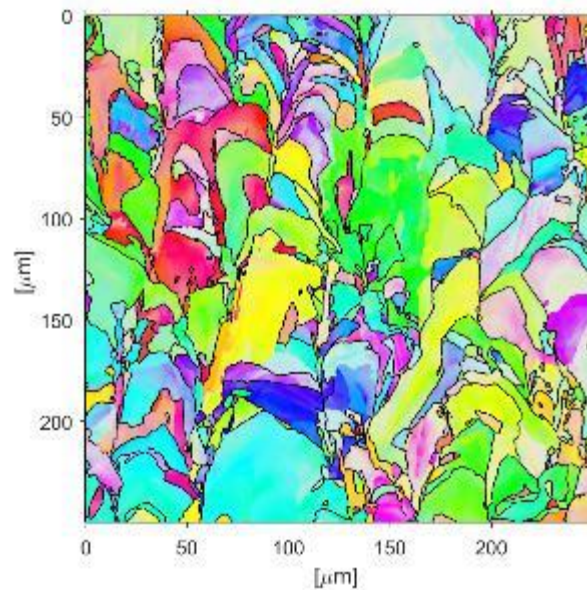


Examples

Band contrast

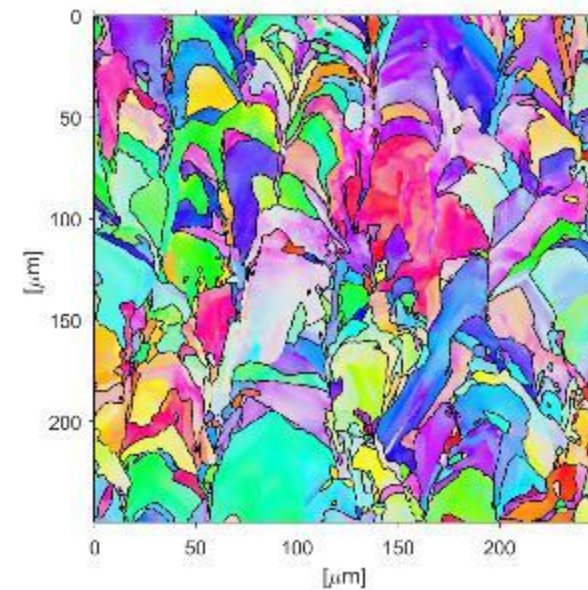


Map Y

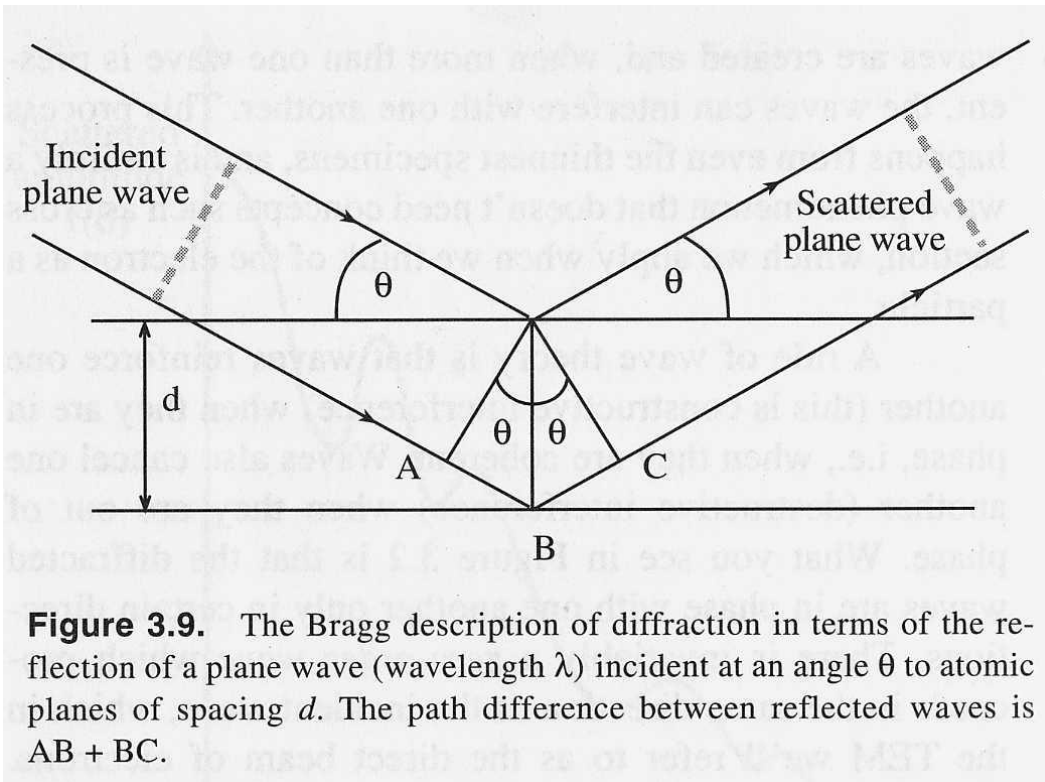


Map Z

Map X



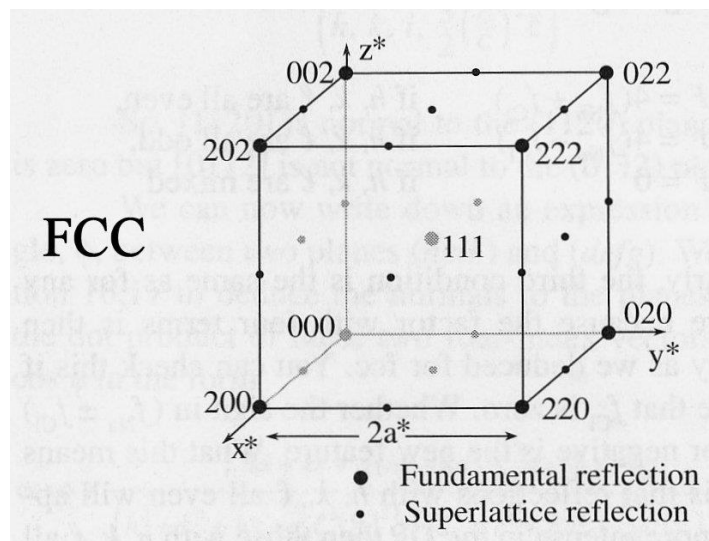
Transmission electron microscopy - diffraction



Bragg law

$$2d_{hkl} \sin \theta = n\lambda$$

Diffraction - reciprocal space



Diffraction is a 2D cut of crystal in reciprocal space

Cubic, tetragonal and orthorhombic lattice

$$\mathbf{a}^* \parallel \mathbf{a} \quad \mathbf{b}^* \parallel \mathbf{b} \quad \mathbf{c}^* \parallel \mathbf{c}$$

$$a^* = 1/a \quad b^* = 1/b \quad c^* = 1/c$$

$$\alpha^* = \beta^* = \gamma^* = \pi/2$$

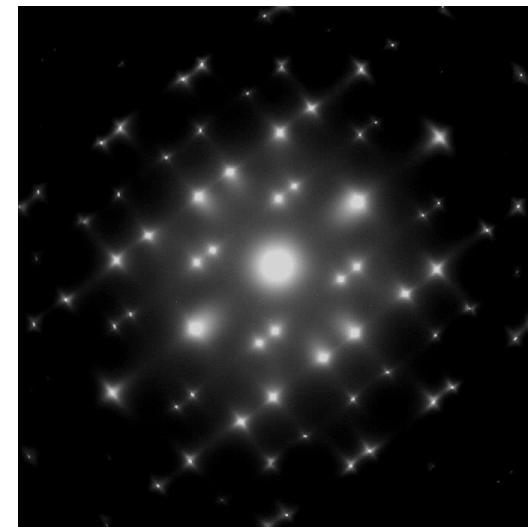
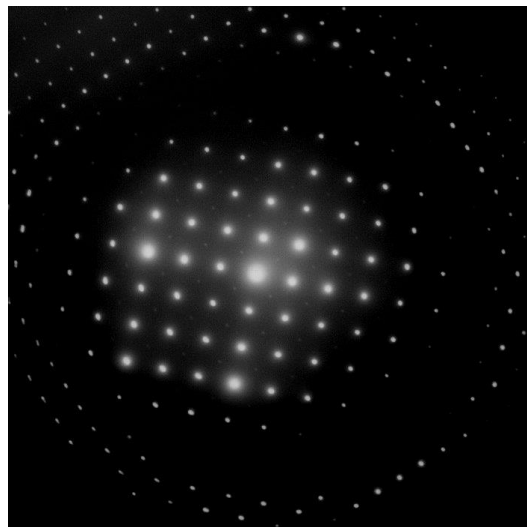
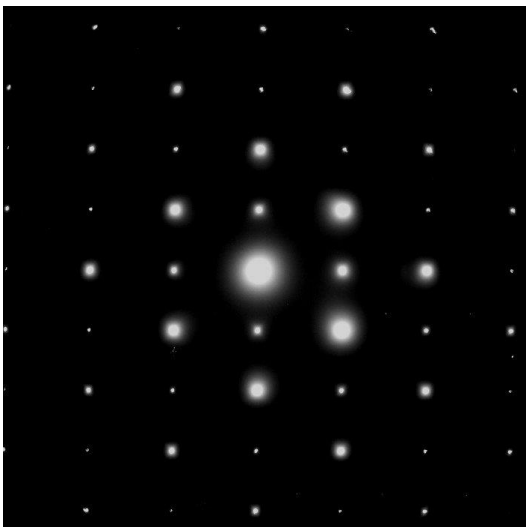
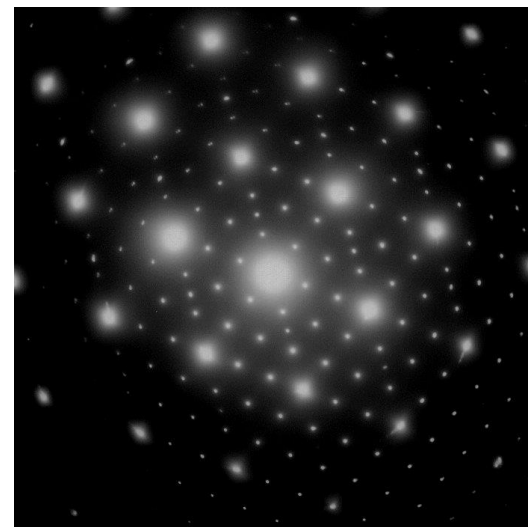
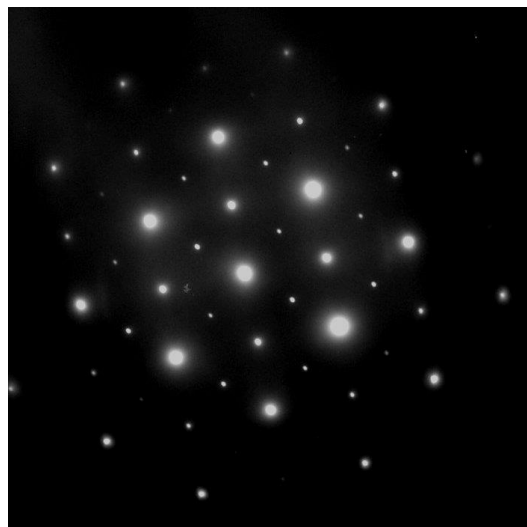
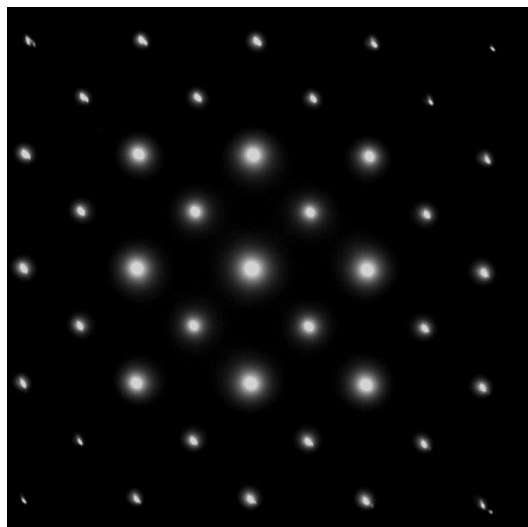
Hexagonal and trigonal lattice

$$\mathbf{c}^* \parallel \mathbf{c} \quad \mathbf{a}^* \text{ and } \mathbf{b}^* \in (\mathbf{a}, \mathbf{b})$$

$$a^* = b^* = 2 / (a\sqrt{3}) \quad c^* = 1/c$$

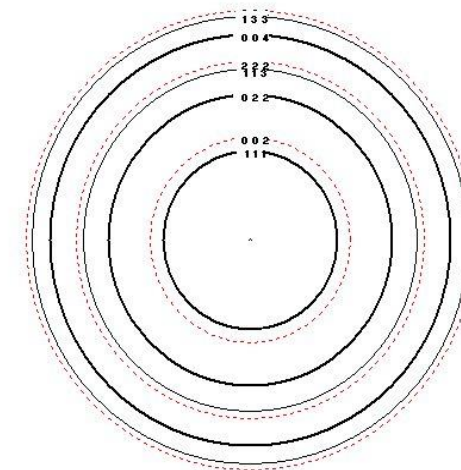
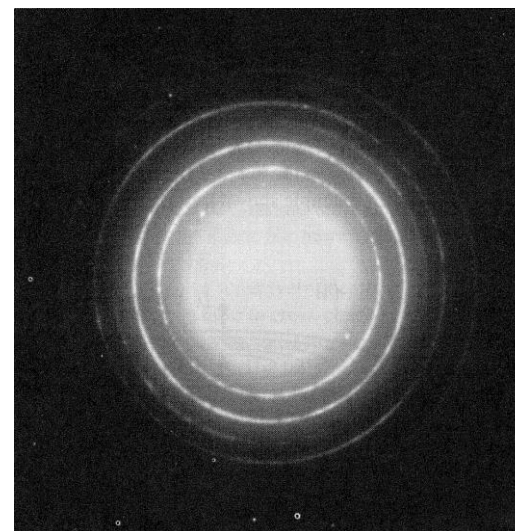
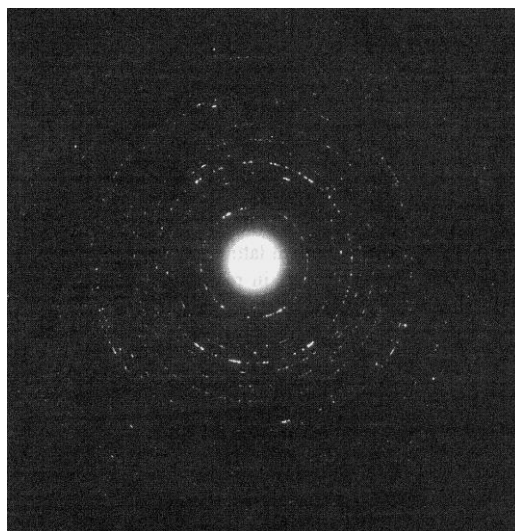
$$\alpha^* = \beta^* = \pi/2 \quad \gamma^* = \pi/3$$

Diffraction patterns – single crystal / one grain



Diffraction patterns

Nanocrystals



Amorphous

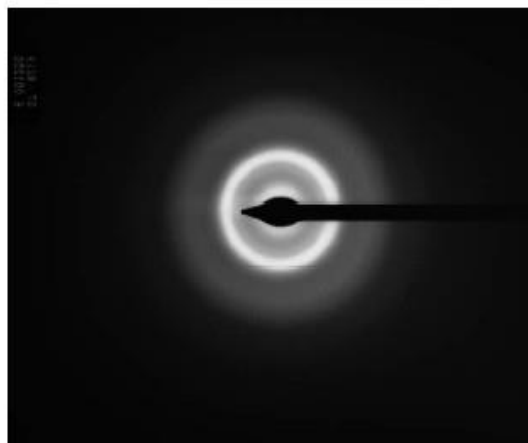


Fig. 3. Electron diffraction pattern taken from the cross section of the 2 mm thick $\text{Cu}_{64}\text{Zr}_{36}$ cast strip. Same result across the whole specimen.

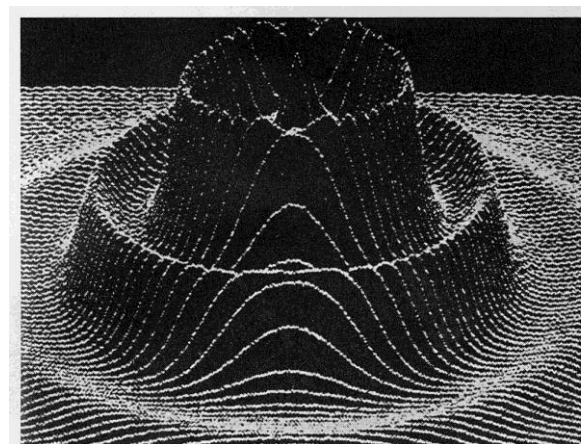


Figure 18.13. A computer plot of the diffracted-intensity distribution from an amorphous structure, showing diffuse rings of intensity. The direct-beam intensity is off scale.

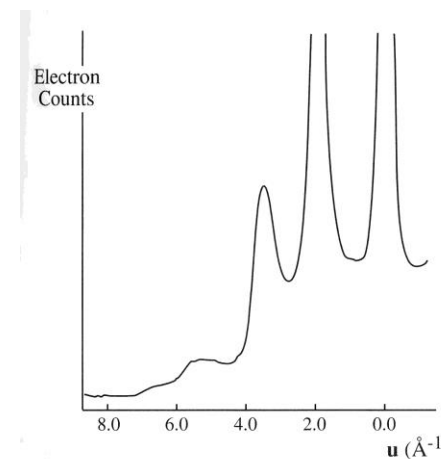


Figure 18.12. An intensity profile across an energy-filtered diffraction pattern from amorphous Si obtained by scanning the pattern across the entrance slit to a serial EELS spectrometer and recording only the elastic (on-axis) electrons.

Transmission electron microscopy – Imaging

$$d\psi_g = i\lambda \frac{F_g n}{\cos \theta} e^{2\pi i \vec{k} \cdot \vec{r}} \equiv q \longrightarrow$$

Kinematic approximation

$$\Phi_g = \int_0^t d\Phi_g = \frac{i\pi}{\xi_g} \frac{\sin(\pi t s_g)}{\pi s_g} \exp(-\pi i s_g t), \longrightarrow I_g \propto \frac{\sin^2(\pi t s_g)}{(s_g \xi_g)^2}$$

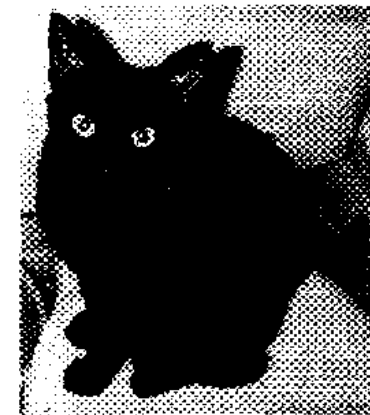
Dynamic theory

$$\frac{d\Phi_g(z)}{dz} = \frac{\pi i}{\xi_0} \Phi_g(z) + \frac{\pi i}{\xi_g} \Phi_0(z) \exp(2\pi i (\vec{\chi} - \vec{\chi}') \cdot \vec{r})$$

$$\frac{d\Phi_0(z)}{dz} = \frac{\pi i}{\xi_0} \Phi_0(z) + \frac{\pi i}{\xi_g} \Phi_g(z) \exp(2\pi i (\vec{\chi}' - \vec{\chi}) \cdot \vec{r})$$

quite complicated....

**Wanted:
\$10,000 Reward**



**Schrödinger's Cat
Dead and Alive**

Transmission electron microscopy – Imaging

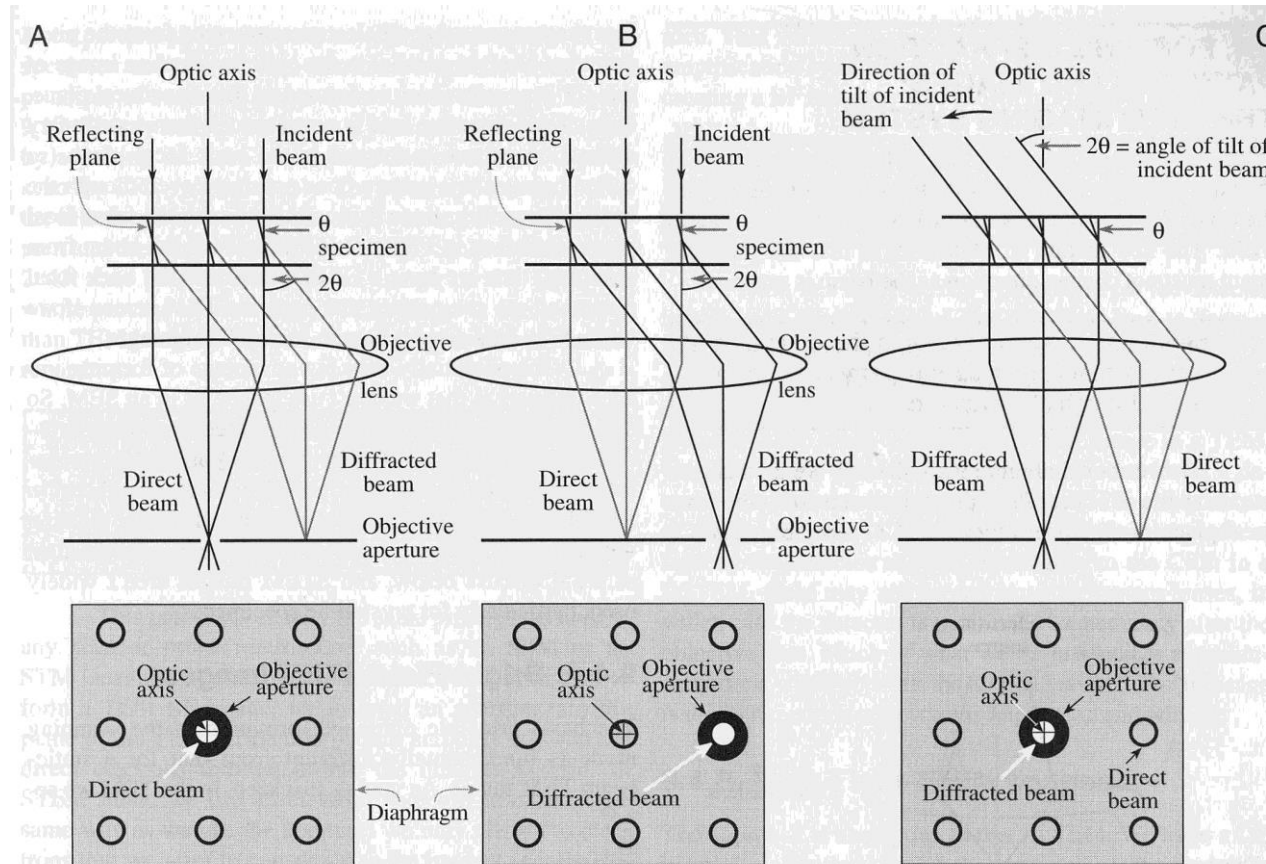
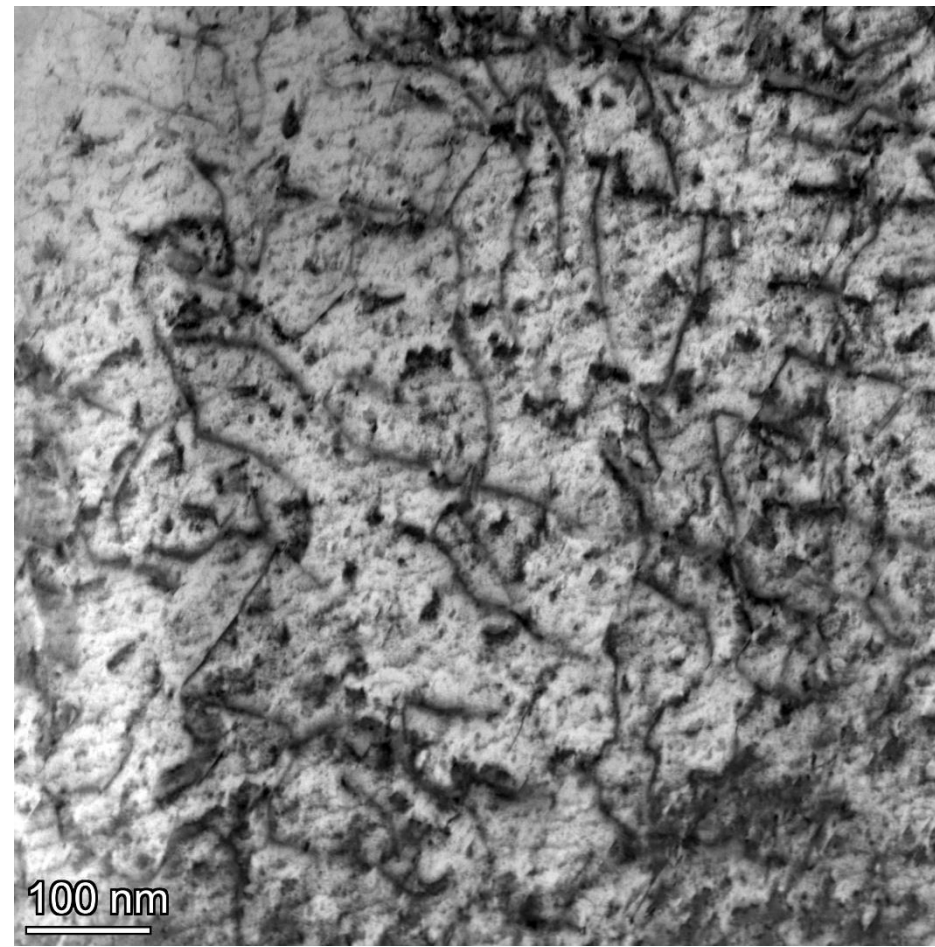
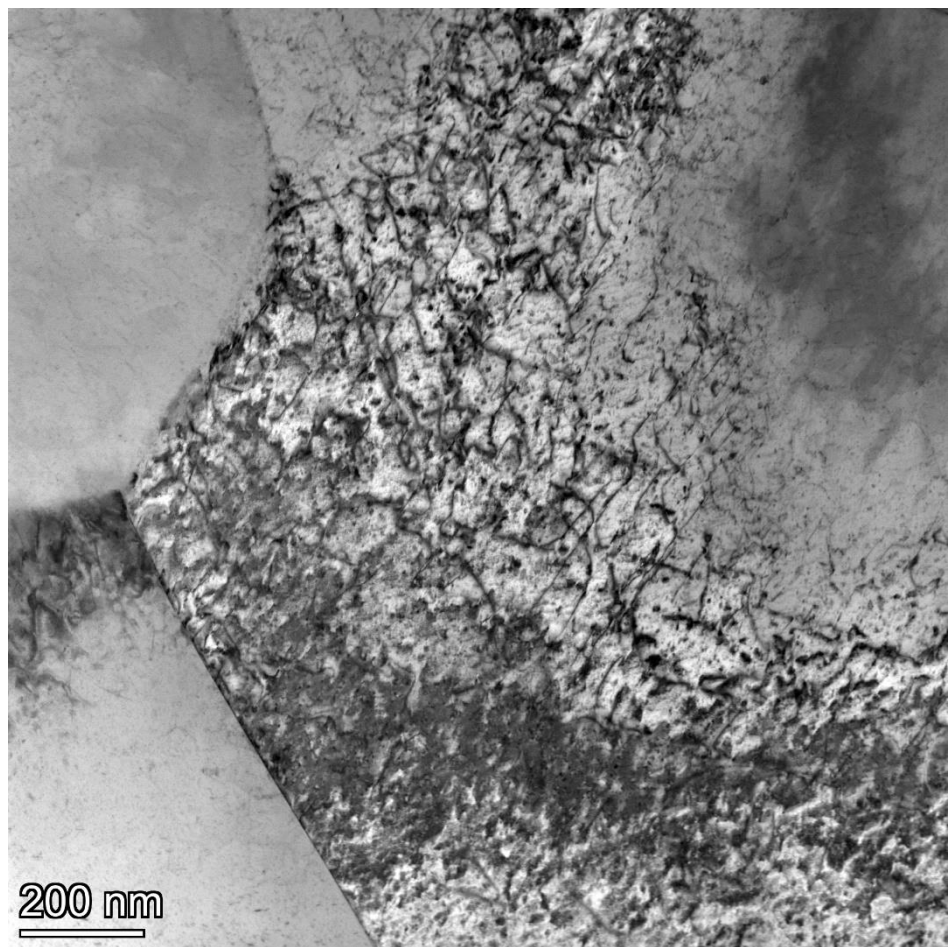


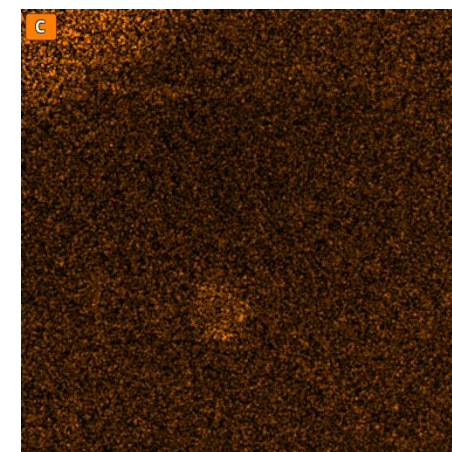
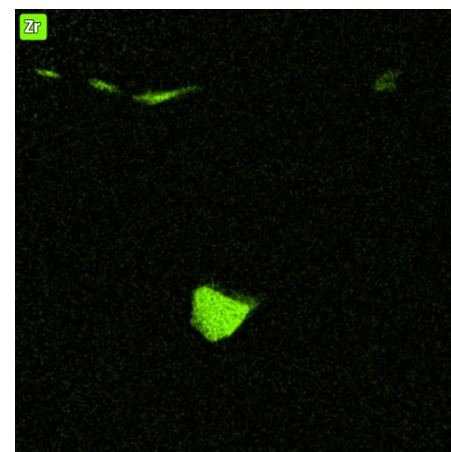
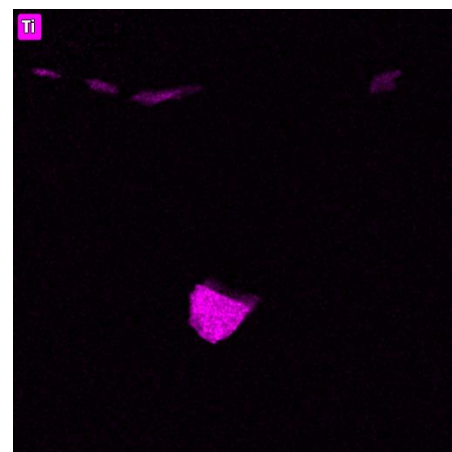
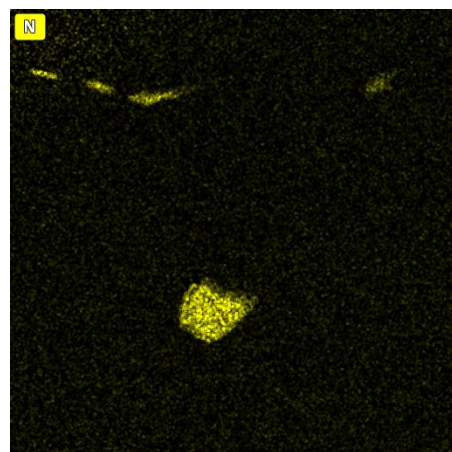
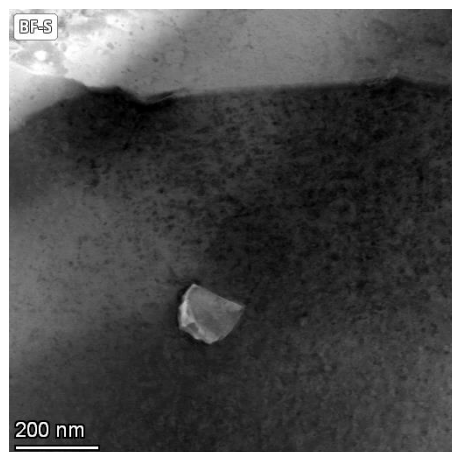
Figure 9.14. Ray diagrams showing how the objective lens/aperture are used in combination to produce (A) a BF image formed from the direct beam, (B) a displaced-aperture DF image formed with a specific off-axis scattered beam, and (C) a CDF image where the incident beam is tilted so that the scattered beam remains on axis. The area selected by the objective aperture, as seen on the viewing screen, is shown below each ray diagram.

TEM – Monel – FIB lamella

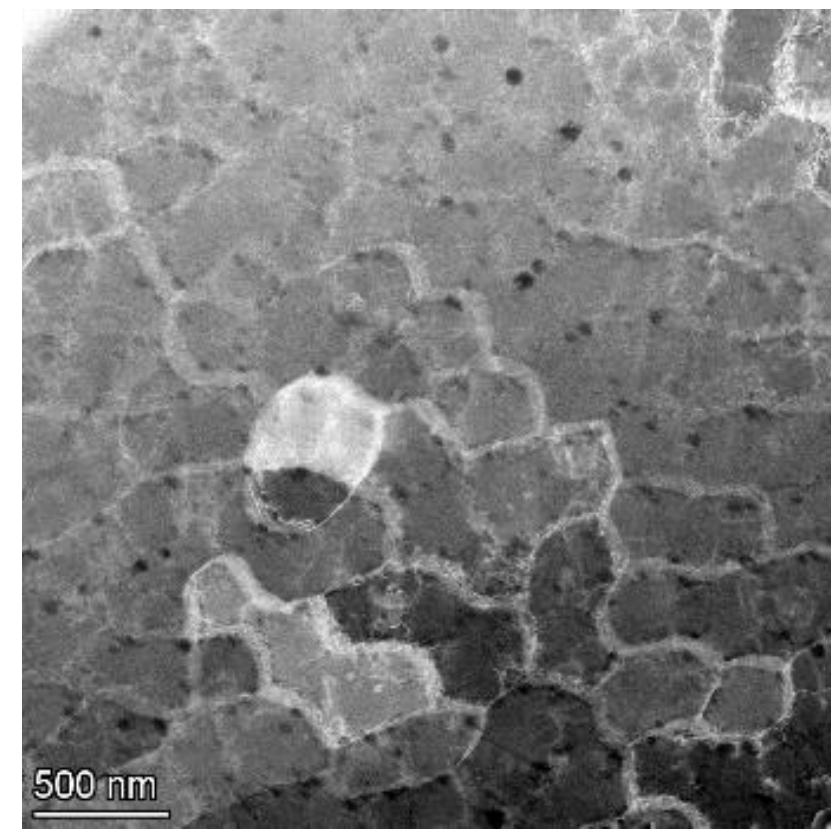
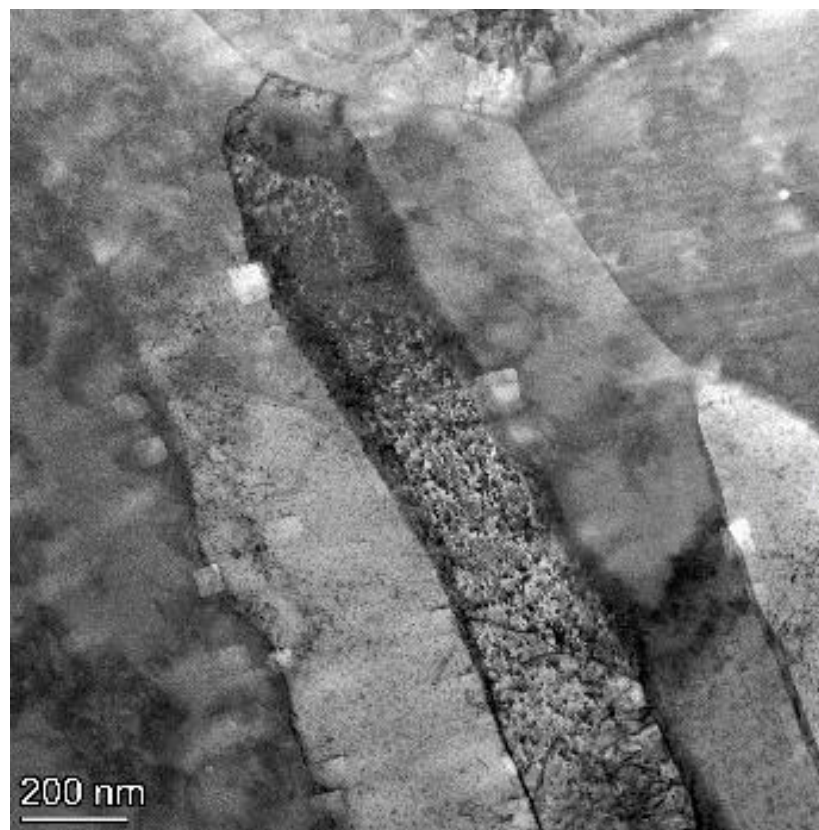
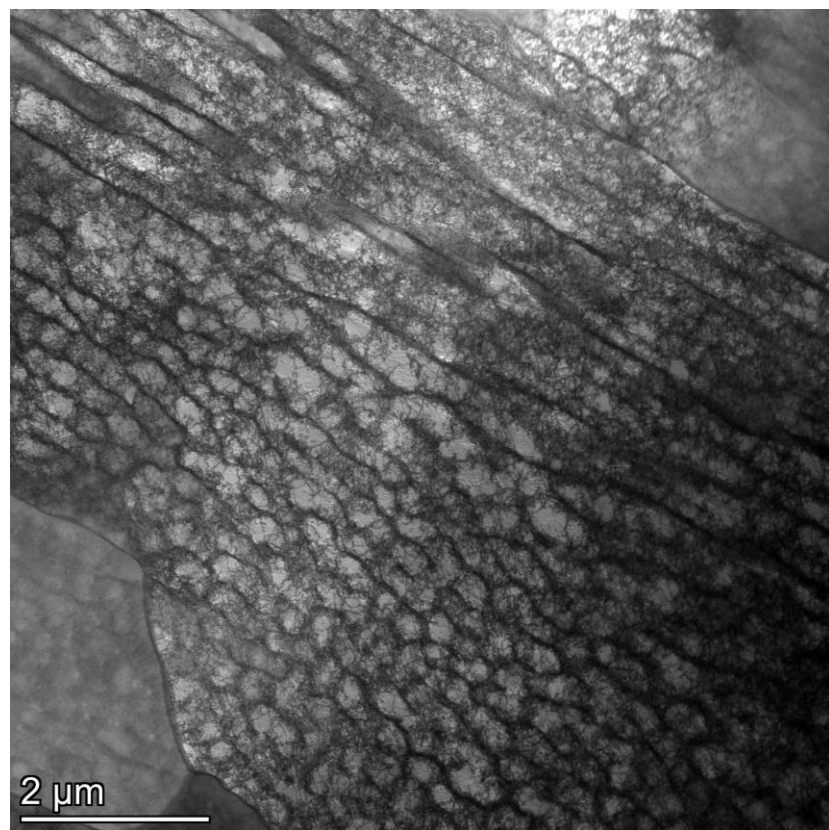


Very high dislocation density. Black dots are probably prismatic dislocation loops

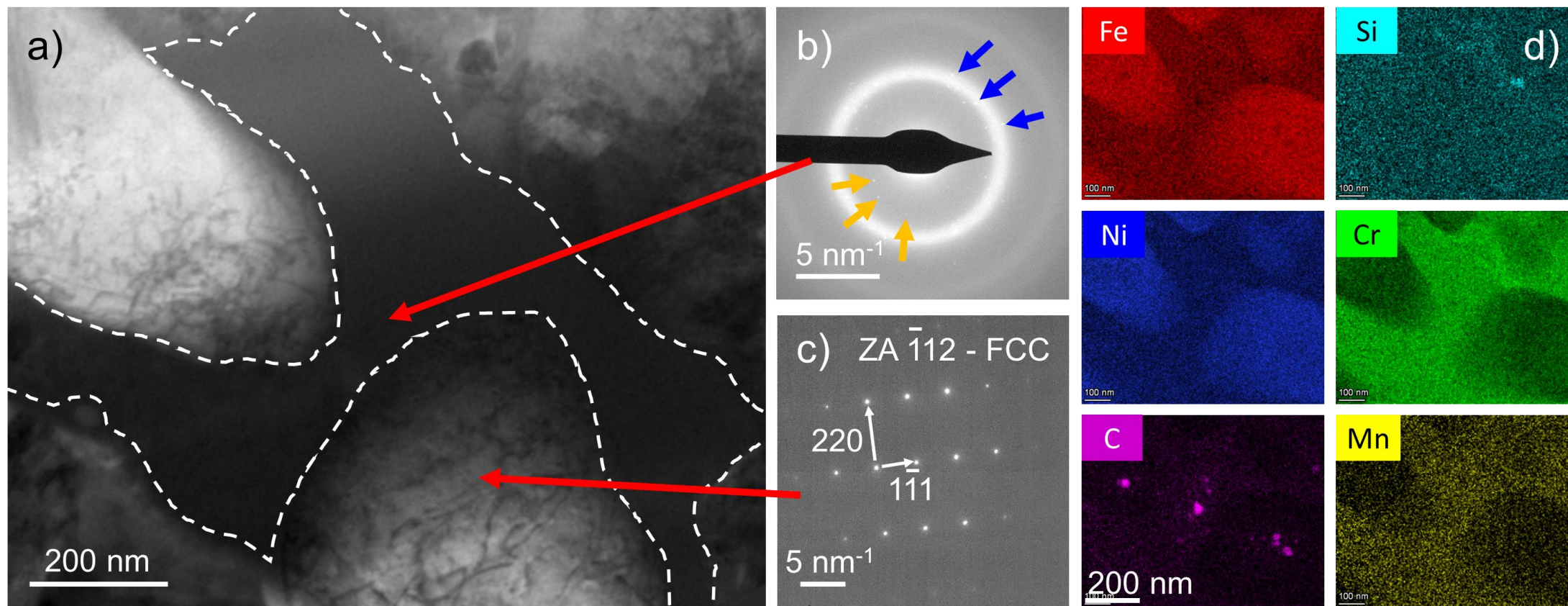
TEM – Kanthal powder



TEM – Monel - bulk



Cold spray - austenitic steel



Cold spray - austenitic steel

